

Control and Optimization of Smart Grid

Steven Low

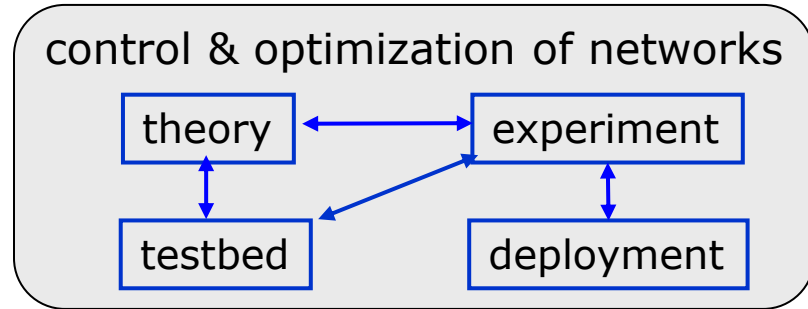
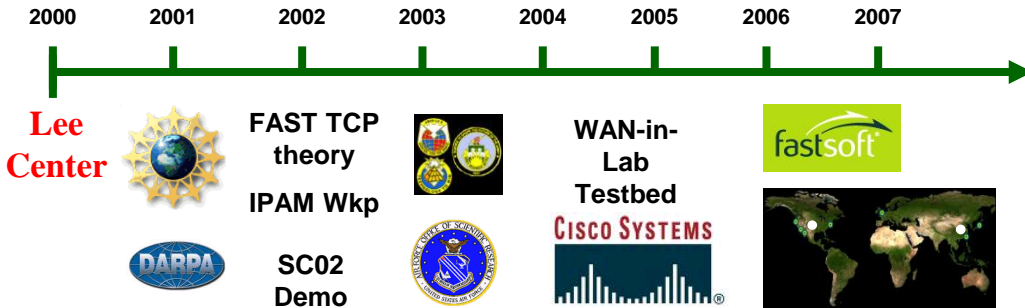
Computing + Math Sciences
Electrical Engineering



Caltech

March 2015
Cornell Ithaca

Caltech FAST Project



Collaborators: Profs Doyle (Caltech), Newman (Caltech), Paganini (Uruguay), Tang (Cornell), Andrew (Swinburne), Chiang (Princeton); CACR, CERN, Internet2, SLAC, Fermi Lab, StarLight, Cisco, Level(3)

theory

Internet: largest distributed nonlinear feedback control system

Reverse engineering: TCP is real-time distributed algorithm over Internet to maximize utility

$$\max_{x \geq 0} \sum U_i(x_i) \quad \text{s.t. } Rx \leq c$$

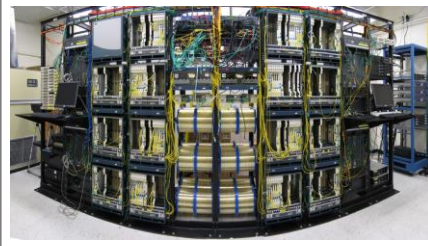
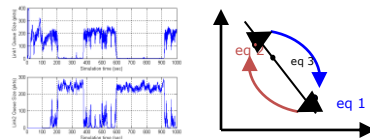
Forward engineering: Invention of FastTCP based on control theory & convex optimization

$$\dot{x}_i = \frac{\gamma_i}{T_i} \left(\alpha_i - x_i(t) \sum_l R_{il} p_l(t) \right)$$

$$\dot{p}_l = \frac{1}{c_l} \left(\sum_i R_{il} x_i(t) - c_l \right)$$

testbed

WAN-in-Lab : one-of-a-kind wind-tunnel in academic networking, with 2,400km of fiber, optical switches, routers, servers, accelerators



experiment

Scientists have used FastTCP to break world records on data transfer between 2002 - 2006

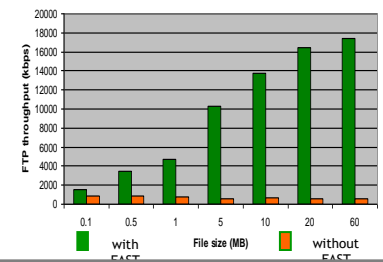
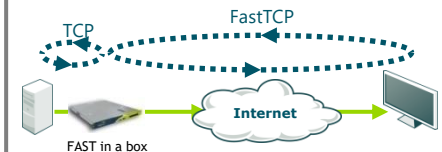


Internet2 LSR SuperComputing BC



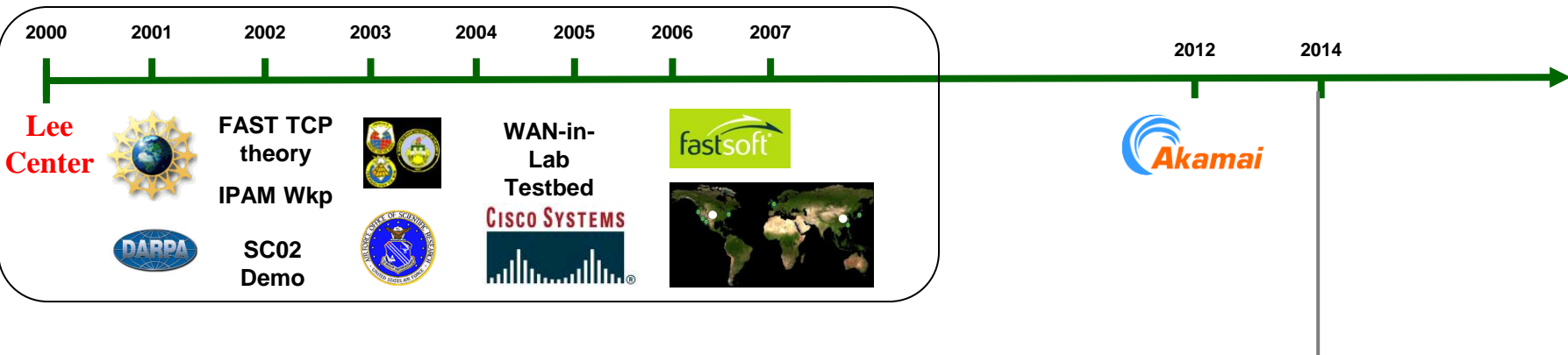
deployment

FAST is commercialized by FastSoft; it accelerates world's 2nd largest CDN and Fortune 100 companies





Caltech FAST Project



accelerating largest social networks, studios, and other Fortune 100 companies



“FAST TCP is accelerating >1TB of internet traffic every second !”



Vision (20+ yrs)

Global energy demand will continue to grow

Traditional supply is unsustainable

There is more **renewable** energy than the world ever needs

- Someone will figure out how to capture and store it

There will be **connected intelligence** everywhere

- Cost of computing, storage, communication and manufacturing will continue to drop

→ Power system will transform into the largest and most complex **Internet of Things**

- Generation, transmission, distribution, consumption, storage



Mission

To develop technologies that will enable and guide the **historic transformation** of our power system

- Generation, transmission, distribution, consumption, storage
- Devices, systems, theory, algorithms
- Control, optimization, stochastics, data, economics



Outline

Overview & challenges

Optimal power flow

Frequency regulation

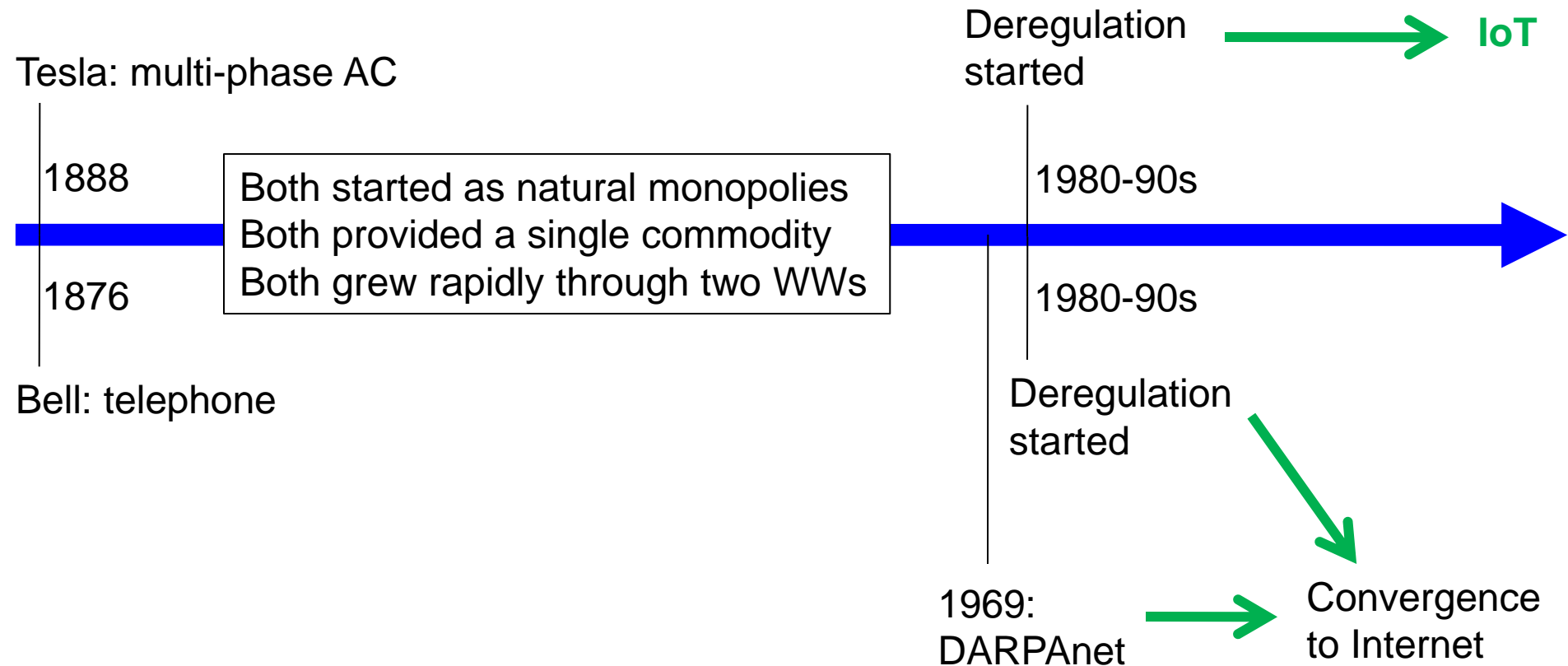
Applications





Watershed moment

Power network will undergo similar architectural transformation that phone network went through in the last two decades





Watershed moment

Industries will be destroyed & created

AT&T, MCI, McCaw Cellular, **Qualcom**

Google, Facebook, Twitter, Amazon, eBay, Netflix

Infrastructure will be reshaped

Centralized intelligence, vertically optimized

Distributed intelligence, layered architecture

What will drive power network transformation ?



Four drivers

Proliferation of renewables

Electrification of transportation

Advances in power electronics

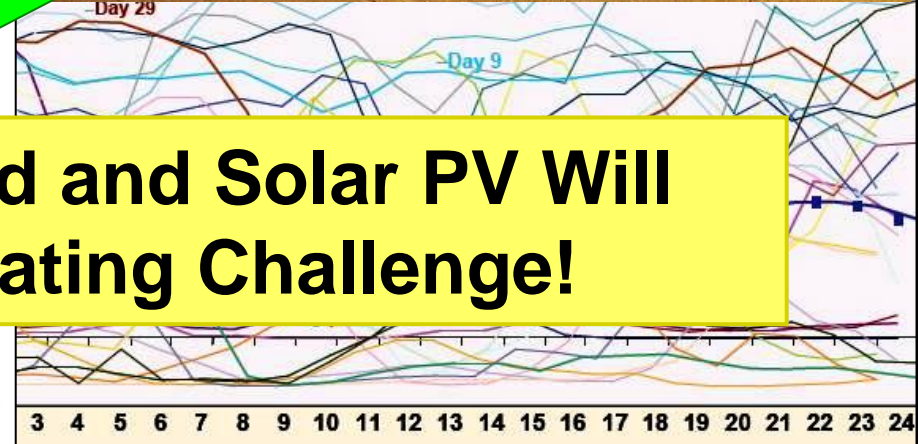
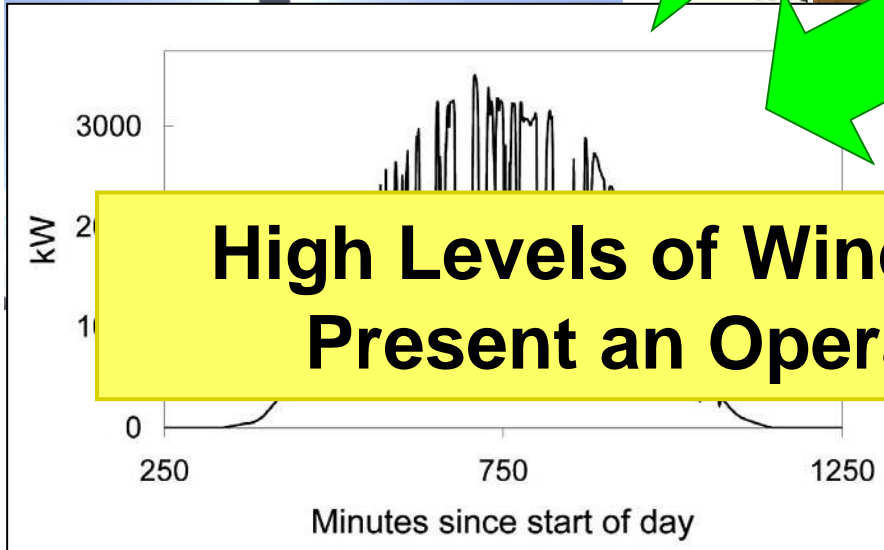
Deployment of sensing, control, comm

} challenges

} enablers

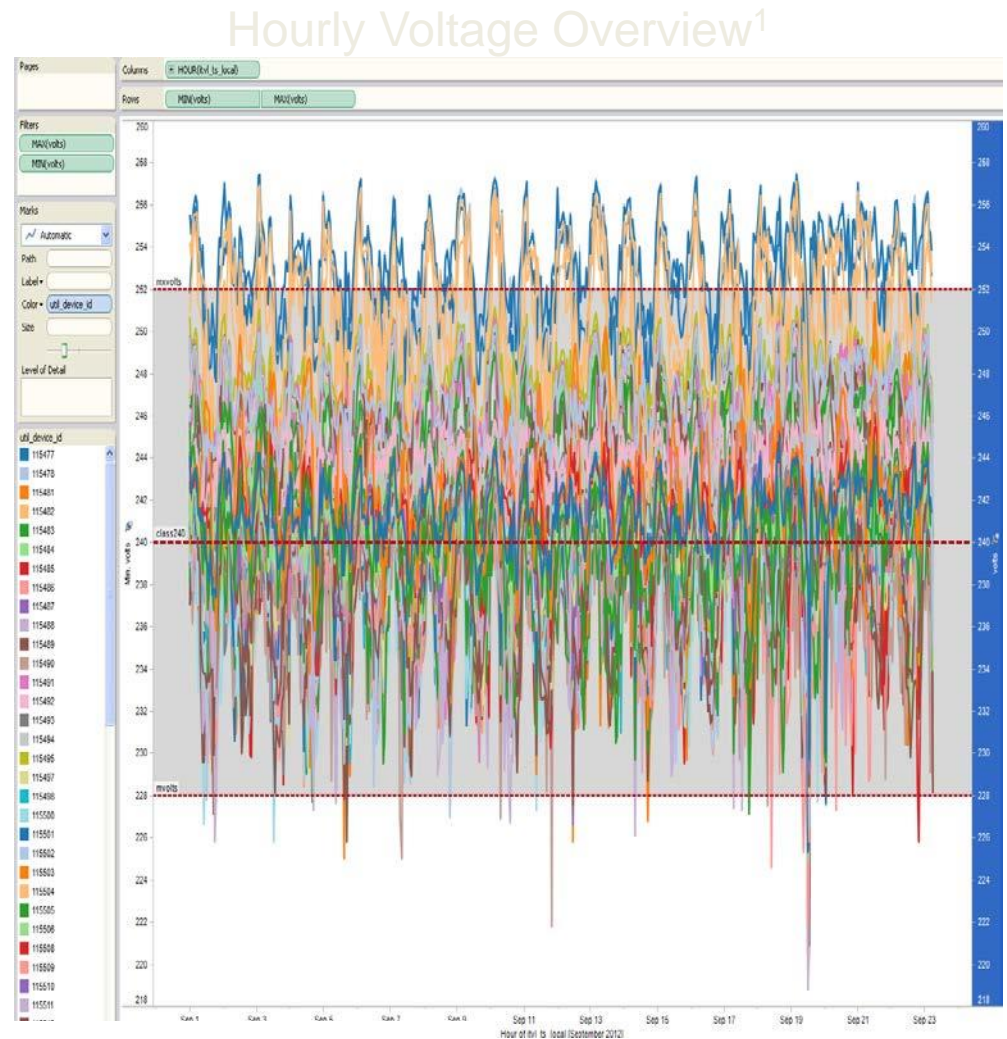


Uncertainty



Source: Rosa Yang, EPRI

- 68 meters (residential)
- Sept 2012 (23 days)
- 240 volts
- +/-5% min-228/max-252
- Hourly by meter #
- A few “high” meters
- Larger # of low meters



Voltage violations are quite frequent



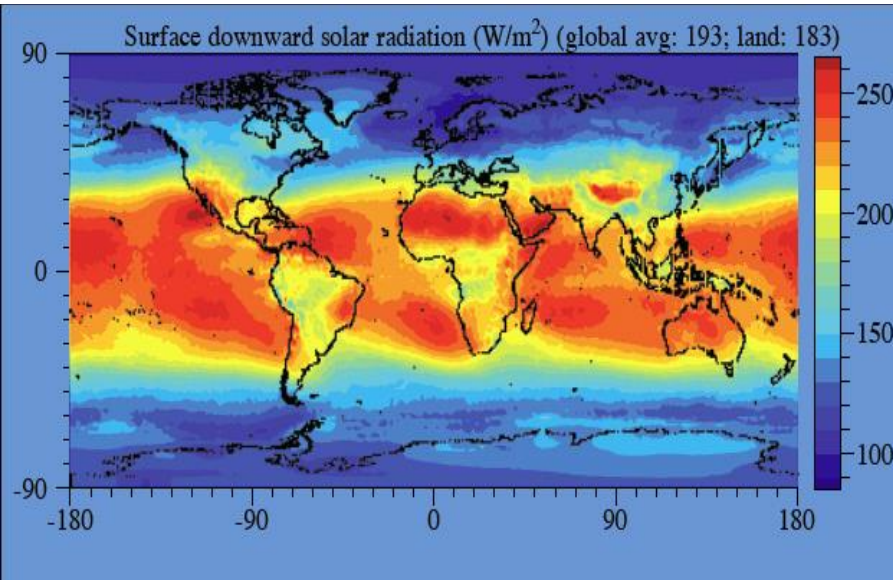
High Penetration

2013

Feb 13-14, San Diego, CA

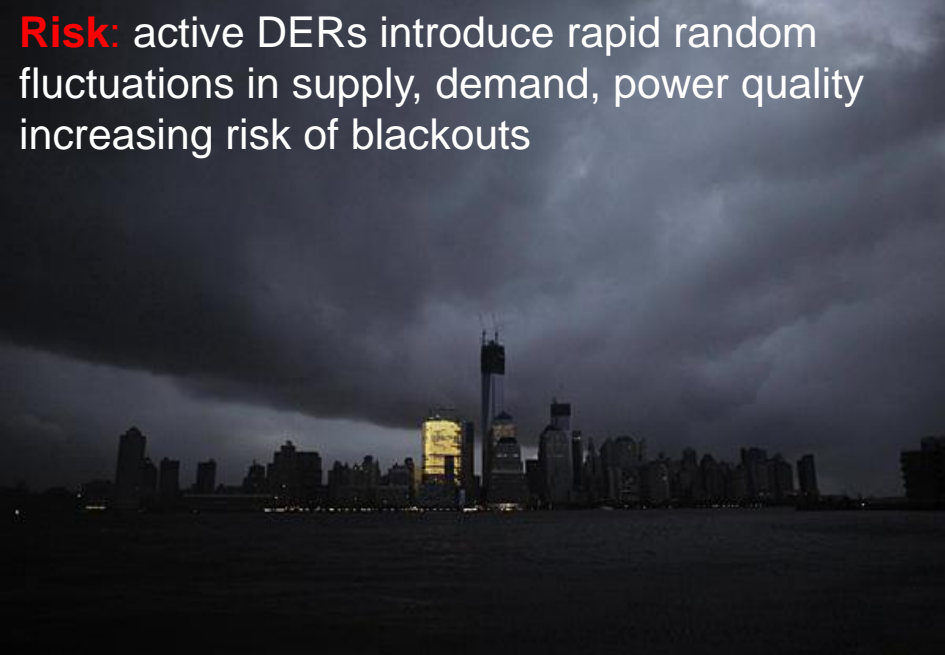
Source: Leon Roose, University of Hawaii
 Development & demo of smart grid inverters for high-penetration PV applications

Solar power over land: > 20x world energy demand



network of
billions of **active**
distributed energy
resources (DERs)

DER: PV, wind tb, EV, storage, smart appliances

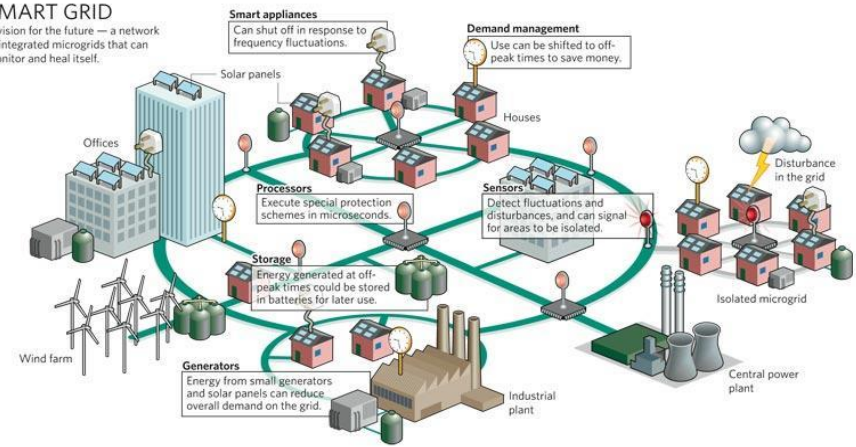


Risk: active DERs introduce rapid random fluctuations in supply, demand, power quality increasing risk of blackouts

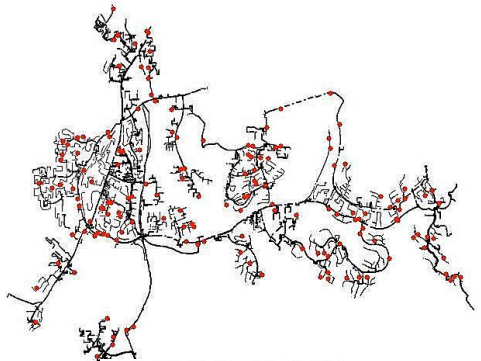
Opportunity: active DERs enables realtime dynamic network-wide feedback control, improving robustness, security, efficiency

SMART GRID

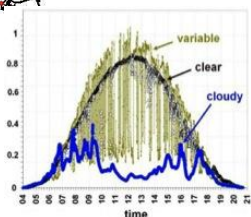
A vision for the future — a network of integrated microgrids that can monitor and heal itself.



Caltech research: distributed control of networked DERs



- Foundational theory, practical algorithms, concrete applications
- Integrate engineering and economics
- Active collaboration with industry





Active DERs: implications

Current control paradigm works well today

- Centralized, open-loop, human-in-loop, worst-case preventive
- Low uncertainty, few active assets to control
- Schedule supplies to match loads

Future needs

- **Closing the loop**, e.g. real-time DR, volt/var
- **Fast computation** to cope with rapid, random, large fluctuations in supply, demand, voltage, freq
- **Simple algorithms** to scale to large networks of active DER
- **Market mechanisms** to incentivize



Need for distributed control

Example: Southern California Edison

- 4-5 million customers

SCE Rossi feeder circuit

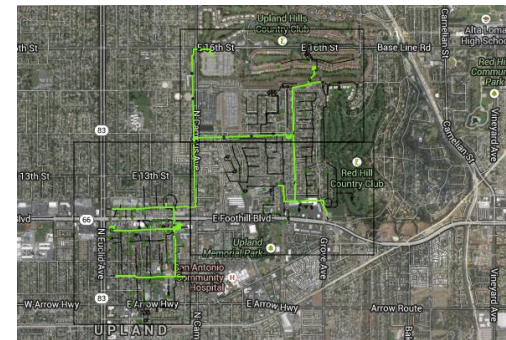
- #houses: 1,407; #commercial/industrial: 131
- #transformers: 422
- #lines: 2,064 (multiphase, inc. transformers)
- peak load: 3 – 6 MW
- #optimization variables: 50,000

SCE has 4,500 feeders

- ~100M variables

United States

- 131M customers, 300K miles of transmission & distr lines, 3,100 utilities





Key challenges

Nonconvexity

- Convex relaxations

Large scale

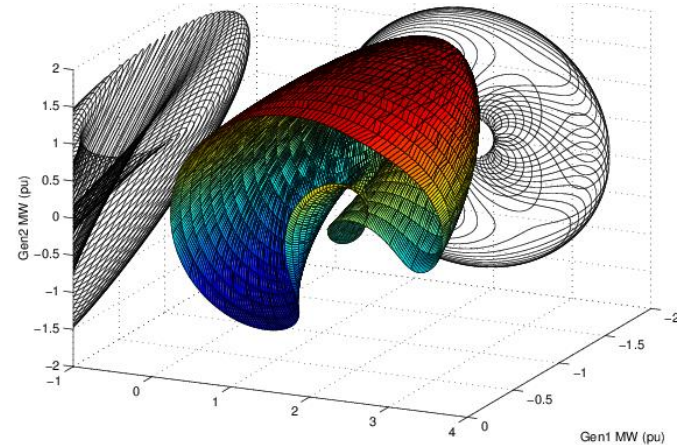
- Distributed algorithms

Uncertainty

- Risk-limiting approach

Multiple timescales

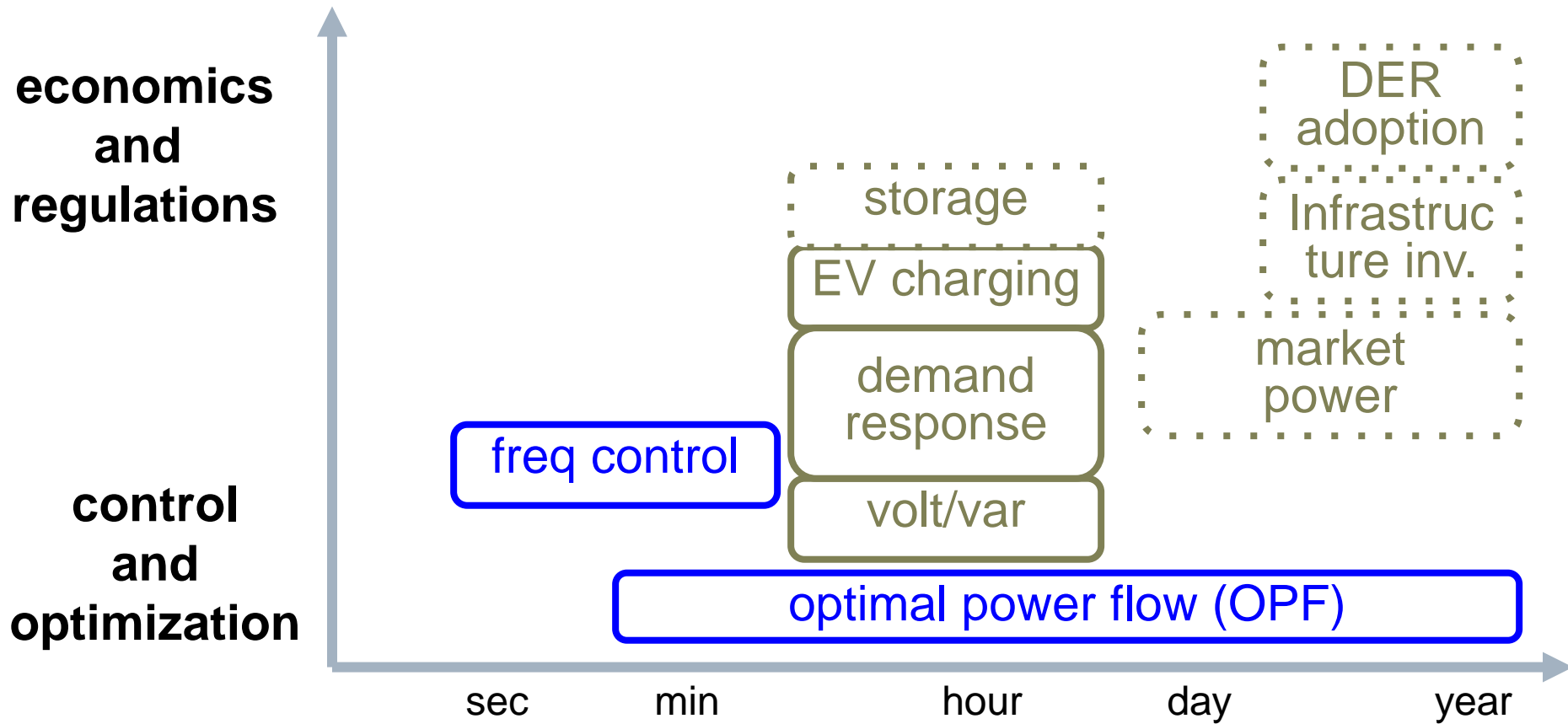
- Decomposition



Ian Hiskens, Michigan



Our research





Outline

Overview & challenges

Optimal power flow (OPF)

- problem formulation
- semidefinite relaxations
- exact relaxation

Frequency regulation

Applications





Optimal power flow (OPF)

OPF is solved routinely for

- network control & optimization decisions
- market operations & pricing
- at timescales of mins, hours, days, ...

Non-convex and hard to solve

- Huge literature since Carpentier 1962
- Common practice: DC power flow (LP)
- Also: Newton-Raphson, interior point, ...



Optimal power flow (OPF)

OPF underlies many applications

- Unit commitment, economic dispatch
- State estimation
- Contingency analysis
- Feeder reconfiguration, topology control
- Placement and sizing of capacitors, storage
- Volt/var control in distribution systems
- Demand response, load control
- Electric vehicle charging
- Market power analysis
- ...



Nonconvexity of OPF

Semidefinite relaxations of power flows

- Physical systems are nonconvex ...
- ... but have hidden convexity that should be exploited

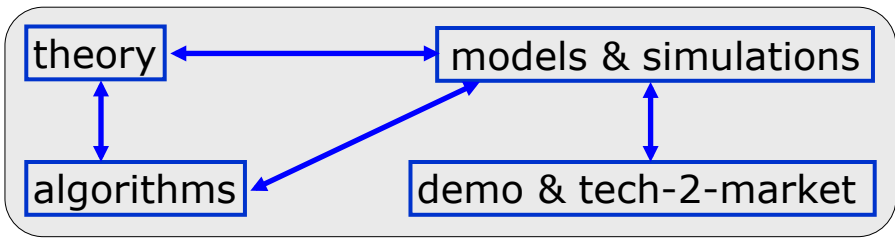
Convexity is important for OPF

- **Foundation** of LMP, critical for efficient market theory
- Required to **guarantee** global optimality
- Required for **real-time** computation at scale

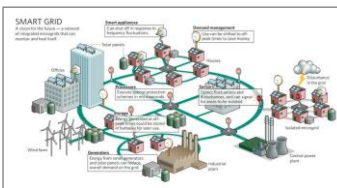


Distributed Control of Networked DER

an **arpa-e** GENI project



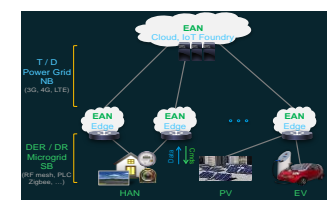
Caltech: Profs Chandy, Doyle, Low (PI); Drs. Bunn, Mallada; Students: Agarwal, Cai, Chen, Farivar, Gan, Guo, Matni, Peng, Ren, Tang, You, Zhao
SCE: Auld, Castaneda, Clarke, Gooding, Montoya, Shah, Sherick (PI)
Newport/Caltech: DeMartini (advisor)
Alumni: Bose (Cornell), Chen (Colorado), Collins (USC), Gayme (JHU), Lavaei (Columbia), Li (Harvard), Topcu (UPenn), Xu (SUTD)



- Increase(asset(u+liza+on(and(efficiency(
- Improve(power(quality(and(stability(
- Move(data:in:mo+on(analy+cs(to(edge(

Contact: Michael Enescu, co-founder CEO, enescu@alumni.caltech.edu

- EAN analytics and optimization
DER placement, asset opt, analytics
- EAN enabled control
DER co-optimization, frequency reg



applications and T2M

theory

Convex relaxation of OPF:
Theoretical foundation for semi-definite relaxations of power flow

OPF: $\min_V \text{tr}(CVV^*)$
 s. t. $\underline{s}_j \in \text{tr}(Y_j^* V V^*) \in \bar{s}_j, \quad v_j \in |V_j|^2 \in \bar{v}_j$

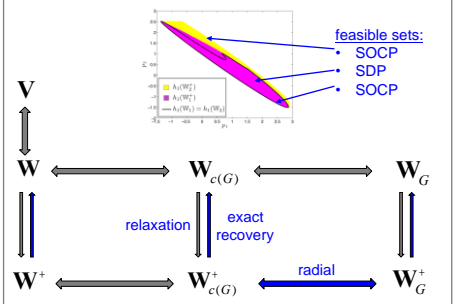
SDP relaxation
 $\min_W \text{tr}(CW)$
 s. t. $\underline{s}_j \in \text{tr}(Y_j^* W) \in \bar{s}_j, \quad \underline{V}_j \in W_{jj} \in \bar{V}_j$
 $W \succeq 0, \quad \text{rank } W = 1$ ignore this (only nonconvex constr)



Exact relaxations: Sufficient conditions for recovering global optimum of OPF from relaxations

algorithms

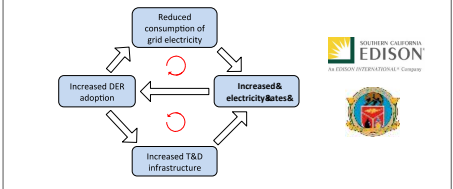
- Relaxation algorithms:**
- single-phase balanced, multiphase unbalanced
 - centralized, distributed



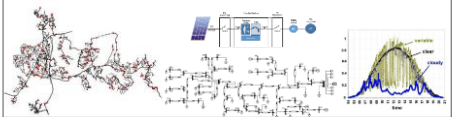
- | | | |
|-----------------------|-----------------------------------|------------------------|
| SDP relaxation | Chordal relaxation | SOCP relaxation |
| • tightest superset | • equivalent superset | • coarsest superset |
| • max # variables | • much faster for sparse networks | • min # variables |
| • slowest | | • fastest |

models

- DER adoption model & software**
- Sophisticated feedback model
 - Cloud service for PV-uptake:
<http://etechuptake.appspot.com/>

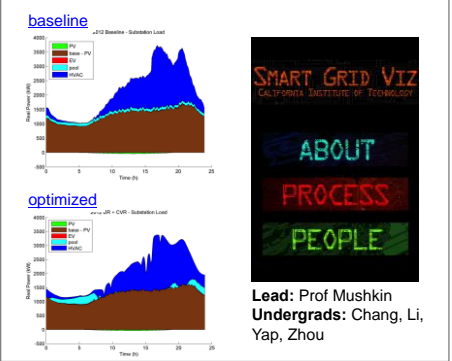


- volt/var control with renewables**
- SCE circuits, DER forecasts
 - advanced OPF solver



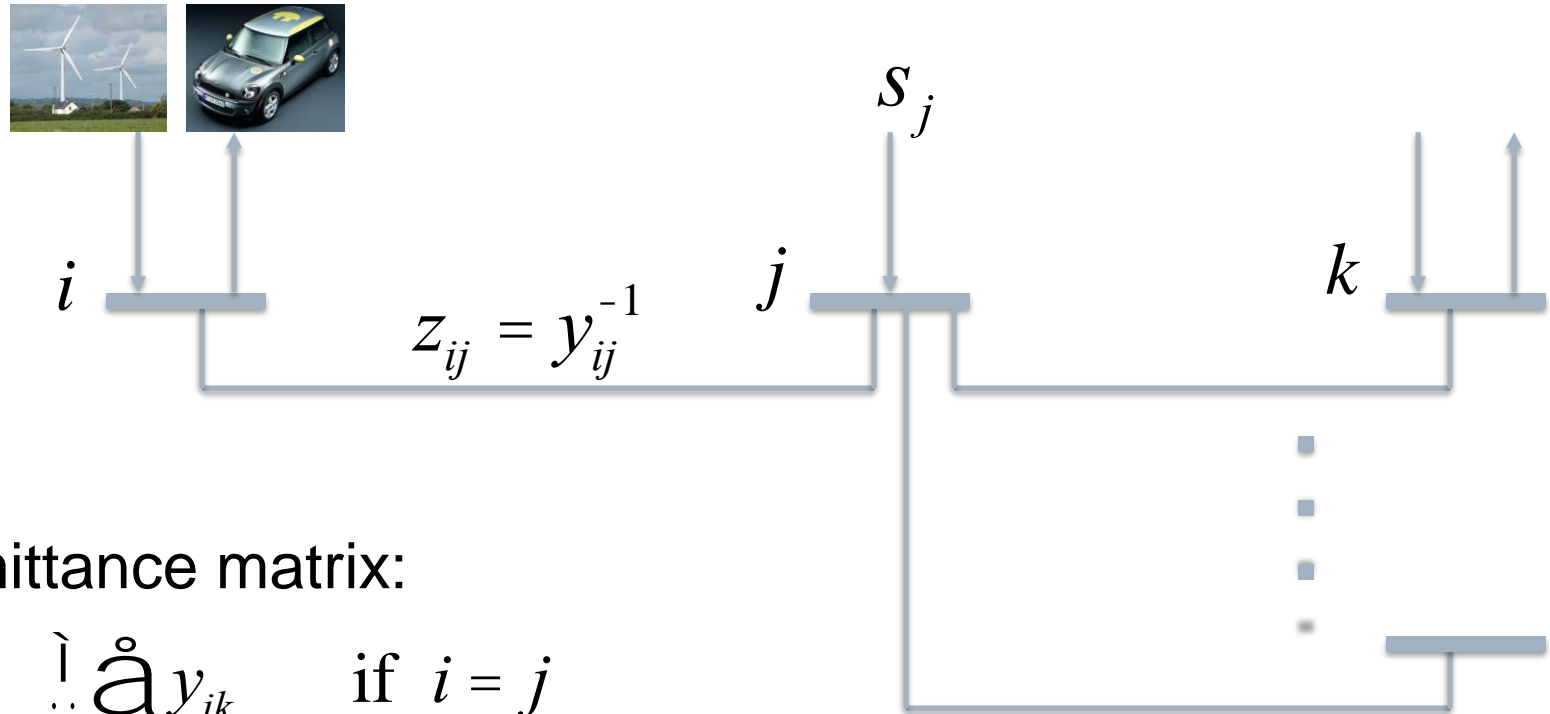
simulations

- Realistic simulations**
- SCE feeder model, 2,000 buses
 - DER: inverters, HVAC, pool pumps, EV
 - Multiphase unbalanced radial





Bus injection model



admittance matrix:

$$Y_{ij} := \begin{cases} \hat{a} y_{ik} & \text{if } i = j \\ -y_{ij} & \text{if } i \sim j \\ 0 & \text{else} \end{cases}$$

graph G : undirected

Y specifies topology of G and impedances z on lines



Bus injection model

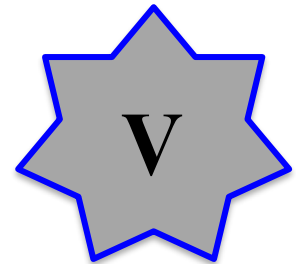
In terms of V :

$$s_j = \text{tr} \left(Y_j^H V V^H \right) \quad \text{for all } j$$

$$Y_j = Y^H e_j e_j^T$$

Power flow problem:

Given (Y, s) find V



isolated solutions



OPF: bus injection model

$$\begin{array}{ll} \min & \text{tr} \left(CVV^H \right) \\ & \text{gen cost,} \\ & \text{power loss} \\ \text{over} & (V, s) \\ \text{subject to} & \underline{s}_j \preceq s_j \preceq \bar{s}_j \quad \underline{V}_j \preceq |V_j| \preceq \bar{V}_j \end{array}$$



OPF: bus injection model

min $\text{tr} (CVV^H)$ gen cost,
power loss

over (V, s)

subject to $\underline{s}_j \preceq s_j \preceq \bar{s}_j$ $\underline{V}_j \preceq |V_j| \preceq \bar{V}_j$

$$s_j = \text{tr} (Y_j^H V V^H)$$

power flow equation



OPF: bus injection model

$$\begin{aligned} \min \quad & \text{tr } CVV^H \\ \text{subject to} \quad & \underline{s}_j \preceq \text{tr} \left(Y_j VV^H \right) \preceq \bar{s}_j \quad \underline{v}_j \preceq |V_j|^2 \preceq \bar{v}_j \end{aligned}$$

nonconvex QCQP
(quad constrained quad program)



Semidefinite relaxations of OPF

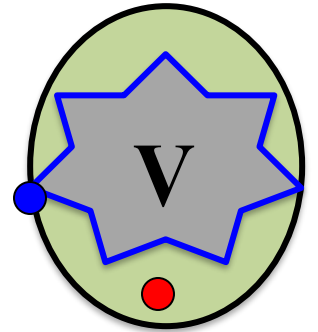
relaxation	model	first proposed	first analyzed
SOCP	BIM	Jabr 2006 TPS	
SDP	BIM	Bai et al 2008 EPES	Lavaei, Low 2012 TPS Bose et al 2011, 2015 Zhang, Tse 2011, 2013 Sojoudi, Lavaei 2012
Chordal	BIM	Bai, Wei 2011 EPES Jabr 2012 TPS	Molzahn et al 2013 TPS Bose et al 2014 TAC
SOCP	BFM	Farivar et al 2011 SGC Farivar, Low 2013 TPS	Farivar et al 2011 SGC Farivar, Low 2013 TPS Gan et al 2012, 2014
Chordal unbalanced	BFM	Gan, Low 2014 PSCC	Gan, Low 2014 PSCC

Tutorial with extensive refs:

Low. Convex relaxation of OPF (I, II), IEEE Trans Control of Network Systems, 2014



Basic idea



$$\begin{array}{l}
 \min \quad \text{tr } CVV^H \\
 \text{subject to} \quad \underline{s}_j \preceq \text{tr} \left(Y_j V V^H \right) \preceq \bar{s}_j \quad \underline{v}_j \preceq |V_j|^2 \preceq \bar{v}_j
 \end{array}$$

$\underbrace{\hspace{15em}}_{\mathbf{V}}$

Approach

1. Three equivalent characterizations of \mathbf{V}
2. Each suggests a lift and relaxation

- What is the relation among different relaxations ?
- When will a relaxation be exact ?



Feasible set & SDP

$$\begin{aligned} \min \quad & \text{tr } CVV^H \\ \text{subject to} \quad & \underline{s}_j \preceq \text{tr} \left(Y_j VV^H \right) \preceq \bar{s}_j \quad \underline{v}_j \preceq |V_j|^2 \preceq \bar{v}_j \end{aligned}$$

quadratic in V
linear in W

Equivalent problem:

$$\begin{aligned} \min \quad & \text{tr } CW \\ \text{subject to} \quad & \underline{s}_j \preceq \text{tr} \left(Y_j W \right) \preceq \bar{s}_j \quad \underline{v}_i \preceq W_{ii} \preceq \bar{v}_i \end{aligned}$$

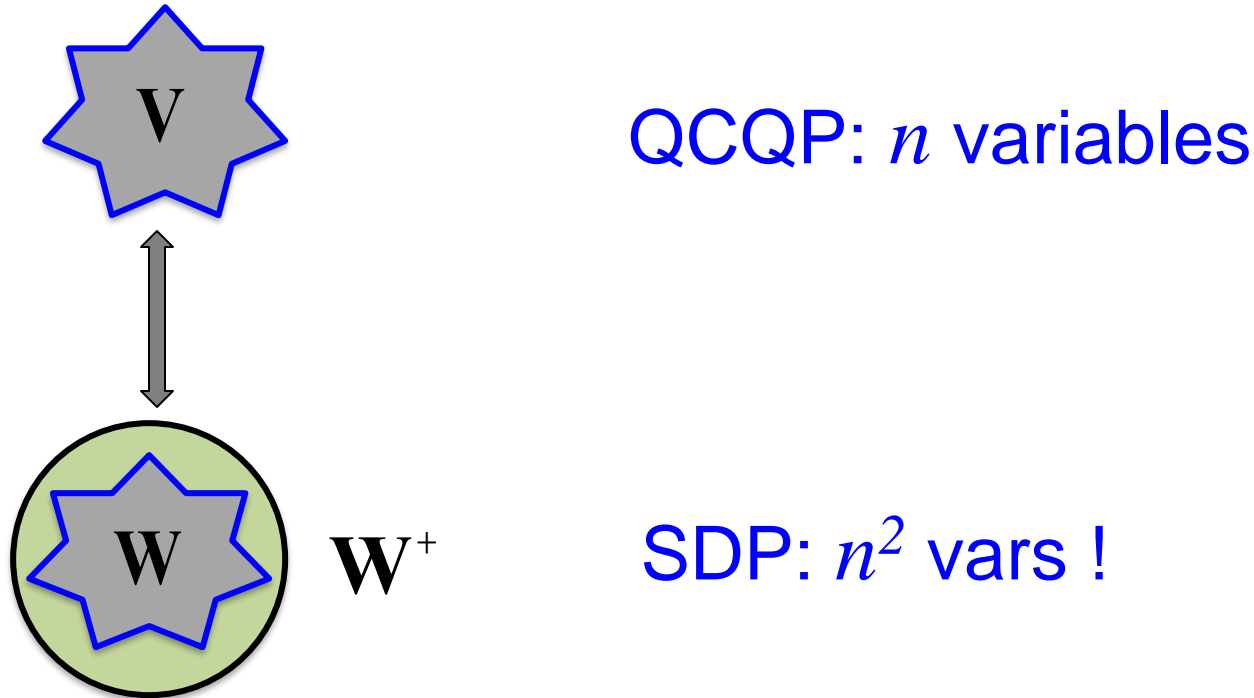
$$W \succeq 0, \text{ rank } W = 1$$

convex in W
except this constraint



Equivalent feasible sets

$$\mathbf{V} := \{V: \underline{\text{quadratic}} \text{ constraints} \}$$



$$\mathbf{W} := \{W: \underline{\text{linear}} \text{ constraints} \} \cap \{W \succeq 0 \text{ ~~rank-1~~}\}$$

idea: $W = VV^H$



Equivalent feasible sets

$$\mathbf{W}_{c(G)} := \left\{ W_{c(G)} : \underline{\text{linear}} \text{ constraints} \right\}$$

$$\text{idea: } W_{c(G)} = \left(VV^H \text{ on } c(G) \right)$$

$$\mathbf{W} := \left\{ W : \underline{\text{linear}} \text{ constraints} \right\} \cap \left\{ W \succeq 0 \text{ rank-1} \right\}$$

$$\text{idea: } W = VV^H$$



Equivalent feasible sets

$$\mathbf{W}_{c(G)} := \left\{ W_{c(G)} : \underline{\text{linear}} \text{ constraints} \right\} \cap \left\{ W_{c(G)} \succeq 0 \text{ rank-1} \right\}$$

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$$\text{idea: } W = VV^H$$



Equivalent feasible sets

$$\mathbf{W}_G := \{W_G : \underline{\text{linear}} \text{ constraints} \}$$

$$\text{idea: } W_G = (VV^H \text{ only on } G)$$

$$\mathbf{W}_{c(G)} := \{W_{c(G)} : \underline{\text{linear}} \text{ constraints} \} \cap \{W_{c(G)} \succeq 0 \text{ rank-1}\}$$

$$\text{idea: } W_{c(G)} = (VV^H \text{ on } c(G))$$

$$\mathbf{W} := \{W : \underline{\text{linear}} \text{ constraints} \} \cap \{W \succeq 0 \text{ rank-1}\}$$

$$\text{idea: } W = VV^H$$



Equivalent feasible sets

$$\mathbf{W}_G := \left\{ W_G : \underline{\text{linear}} \text{ constraints} \right\} \cap \left\{ \begin{array}{l} W(j,k) \geq 0 \text{ rank-1,} \\ \text{cycle cond on } \angle W_{jk} \end{array} \right\}$$

$$\text{idea: } W_G = (VV^H \text{ only on } G)$$

$$\mathbf{W}_{c(G)} := \left\{ W_{c(G)} : \underline{\text{linear}} \text{ constraints} \right\} \cap \left\{ W_{c(G)} \geq 0 \text{ rank-1} \right\}$$

$$\text{idea: } W_{c(G)} = (VV^H \text{ on } c(G))$$

$$\mathbf{W} := \left\{ W : \underline{\text{linear}} \text{ constraints} \right\} \cap \left\{ W \geq 0 \text{ rank-1} \right\}$$

$$\text{idea: } W = VV^H$$



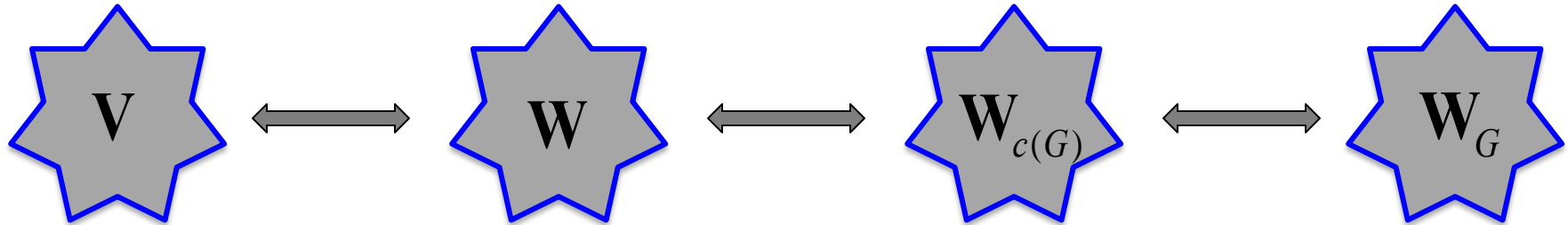
Cycle condition

local $W_G(j, k) \succeq 0$, $\text{rank } W_G(j, k) = 1$, $(j, k) \in E$,

global $\sum_{(j,k) \in c} \mathfrak{D}[W_G]_{jk} = 0 \pmod{2\pi}$ \leftarrow cycle cond



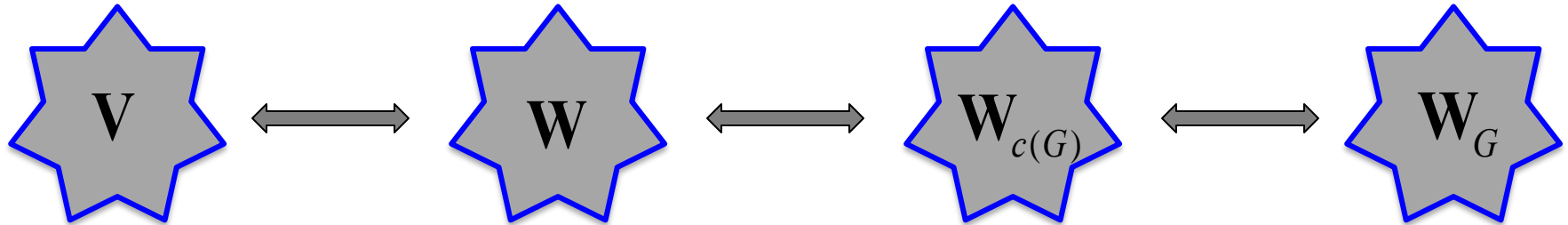
Equivalent feasible sets



Theorem: $V \circ W \circ W_{c(G)} \circ W_G$



Equivalent feasible sets



Theorem: $V \circ W \circ W_{c(G)} \circ W_G$

Given $W_G \hat{=} W_G$ or $W_{c(G)} \hat{=} W_{c(G)}$ there is **unique** completion $W \hat{=} W$ and unique $V \hat{=} V$

Can minimize cost over **any** of these sets, but ...



Equivalent feasible sets

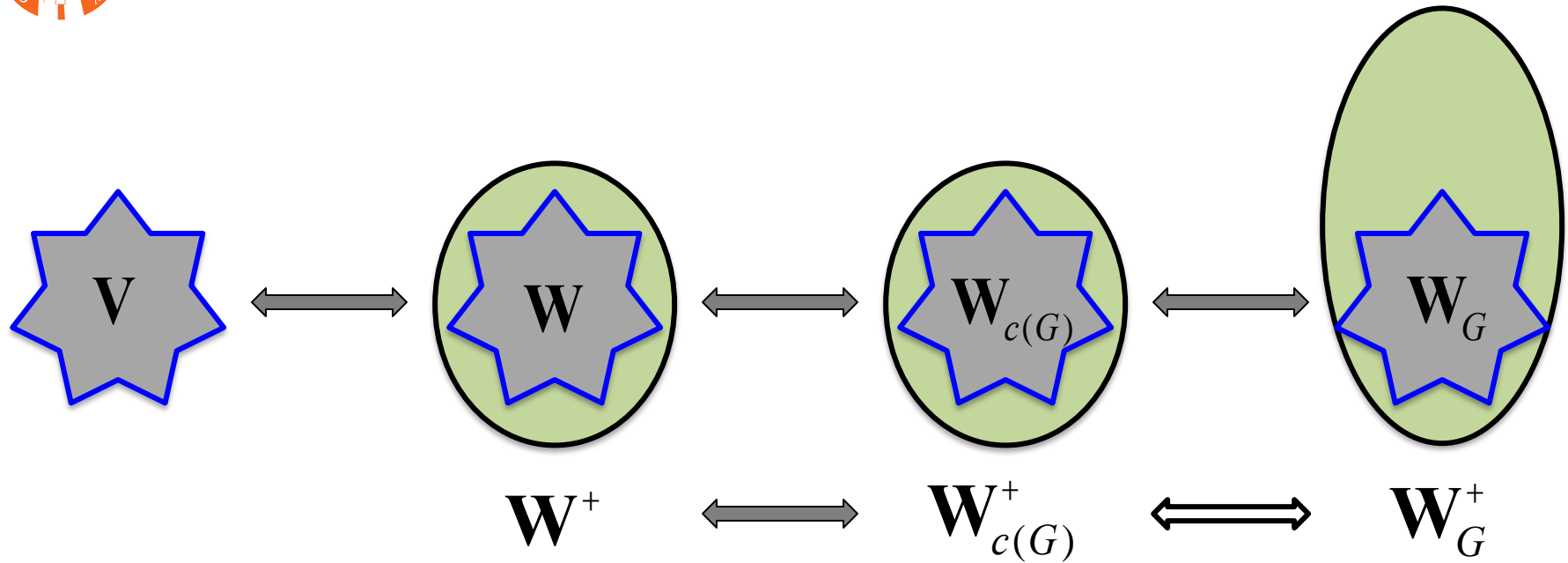
$$\mathbf{W}_G := \left\{ W_G : \underline{\text{linear}} \text{ constraints} \right\} \cap \left\{ \begin{array}{l} W(j,k) \geq 0 \text{ ~~rank-1~~,} \\ \text{~~cycle cond on } \angle W_{jk} \end{array} \right\}~~$$

$$\mathbf{W}_{c(G)} := \left\{ W_{c(G)} : \underline{\text{linear}} \text{ constraints} \right\} \cap \left\{ W_{c(G)} \geq 0 \text{ ~~rank-1~~} \right\}$$

$$\mathbf{W} := \left\{ W : \underline{\text{linear}} \text{ constraints} \right\} \cap \left\{ W \geq 0 \text{ ~~rank-1~~} \right\}$$



Relaxations

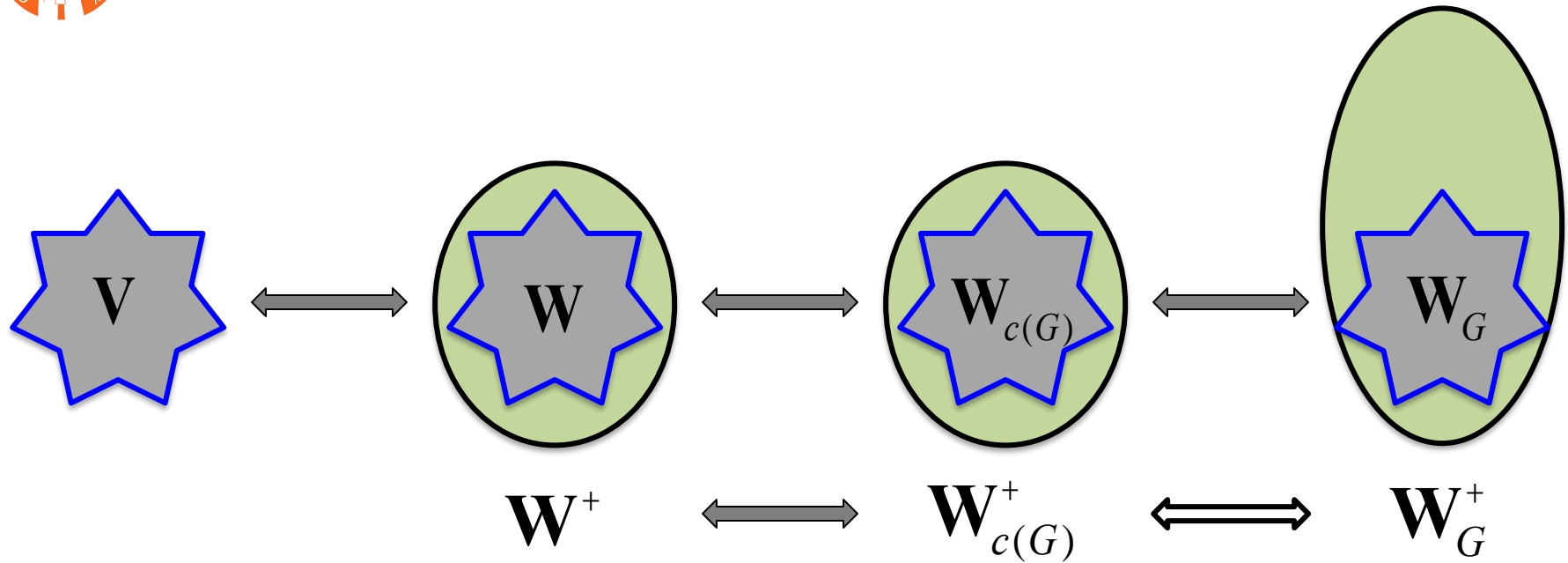


Theorem

- Radial G : $V \subseteq W^+ @ W_{c(G)}^+ @ W_G^+$
- Mesh G : $V \subseteq W^+ @ W_{c(G)}^+ \subseteq W_G^+$



Relaxations



Theorem

- Radial G : $V \subseteq W^+ @ W_{c(G)}^+ @ W_G^+$
- Mesh G : $V \subseteq W^+ @ W_{c(G)}^+ \subseteq W_G^+$

For radial networks: always solve SOCP !



Recap: semidef relaxations

OPF

$$\min_V C(V) \quad \text{subject to } V \hat{=} \mathbf{V}$$

OPF-sdp:

$$\min_W C(W_G) \quad \text{subject to } W \in \mathbb{W}^+$$

OPF-ch:

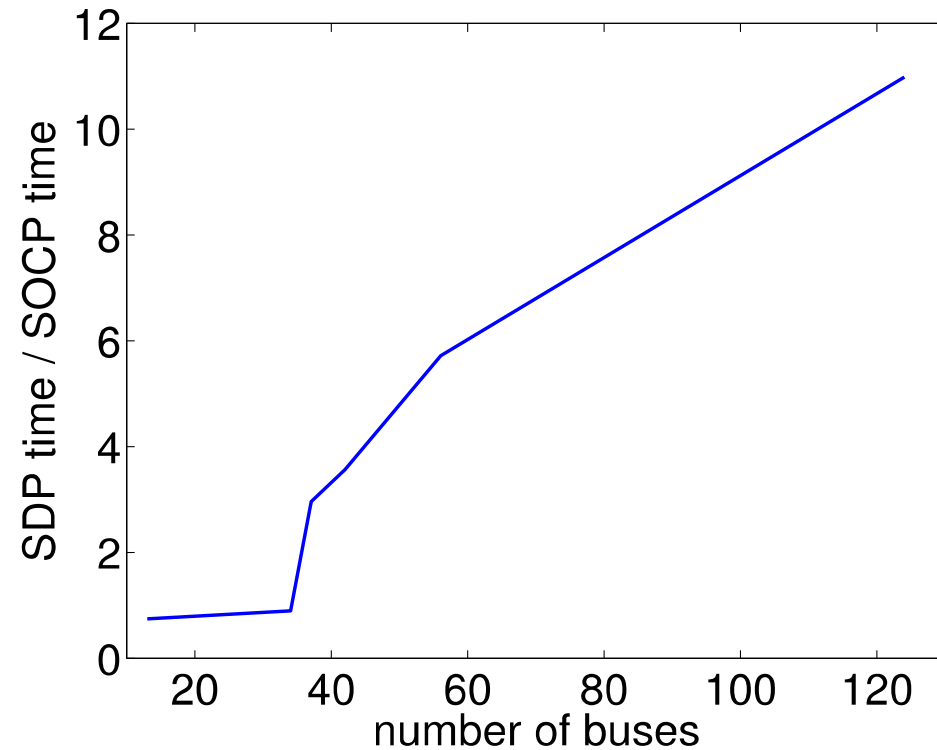
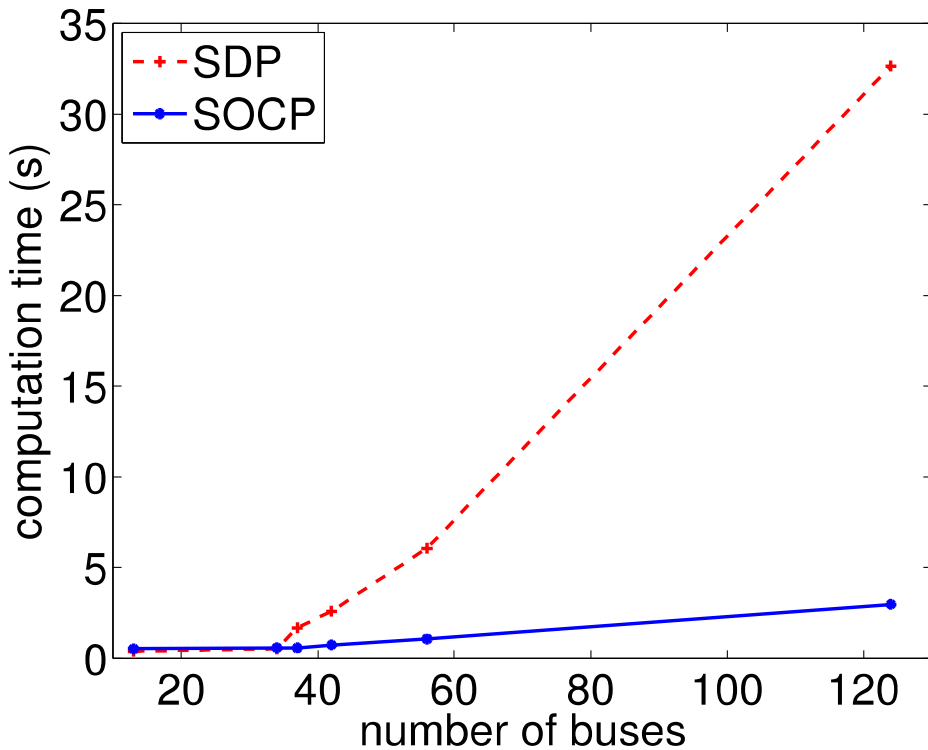
$$\min_{W_{c(G)}} C(W_G) \quad \text{subject to } W_{c(G)} \in \mathbb{W}_{c(G)}^+$$

OPF-socp:

$$\min_{W_G} C(W_G) \quad \text{subject to } W_G \in \mathbb{W}_G^+$$



SOCP more efficient than SDP

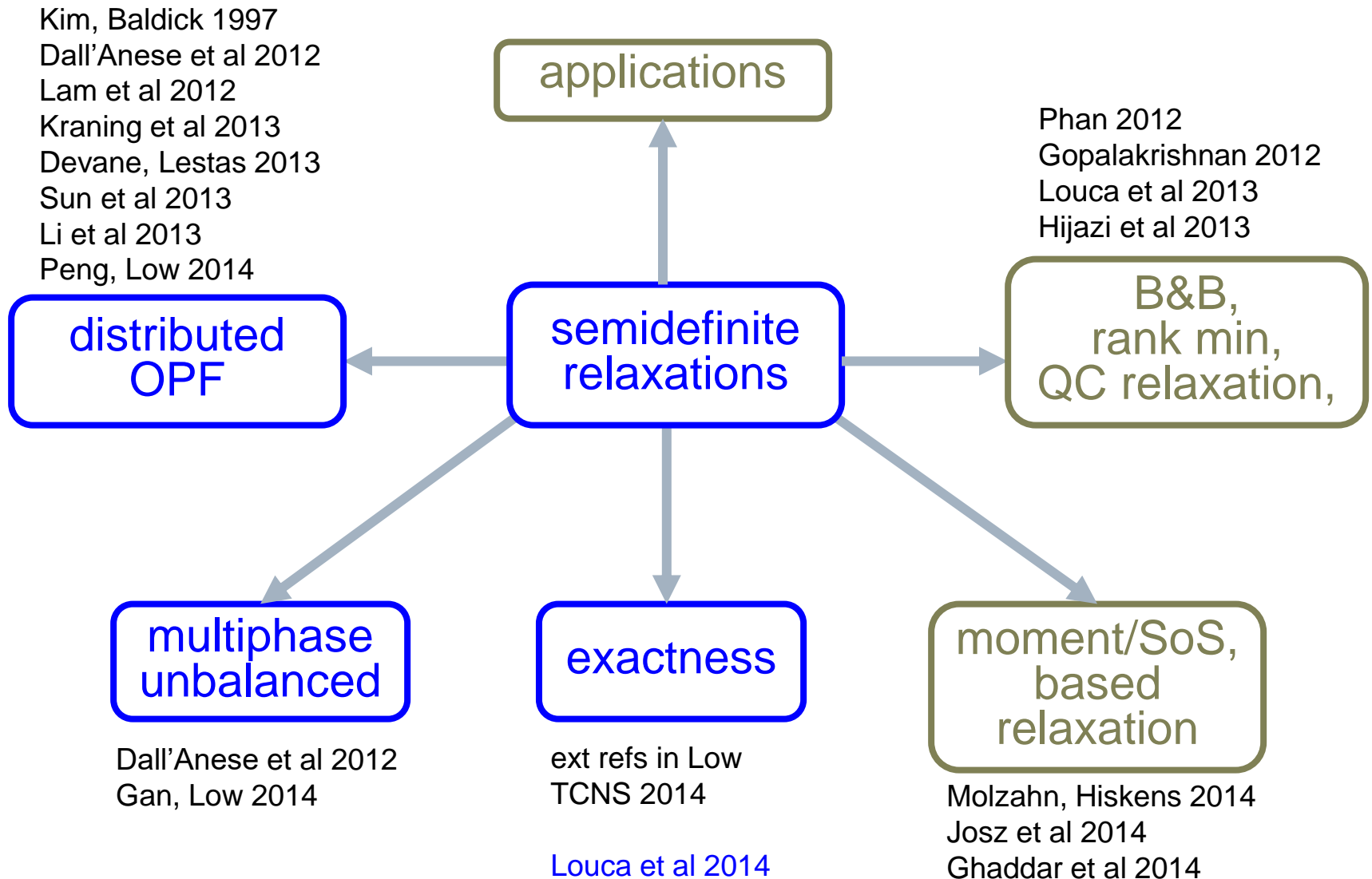


Relaxations are exact in all cases

- IEEE networks: IEEE 13, 34, 37, 123 buses (0% DG)
- SCE networks 47 buses (57% PV), 56 buses (130% PV)
- Single phase; SOCP using BFM
- Matlab 7.9.0.529 (64-bit) with CVX 1.21 on Mac OS X 10.7.5 with 2.66GHz Intel Core 2 Duo CPU and 4GB 1067MHz DDR3 memory



OPF: extensions





Outline

Overview & challenges

Optimal power flow (OPF)

Frequency regulation

- load-side participation
- algorithm design and stability

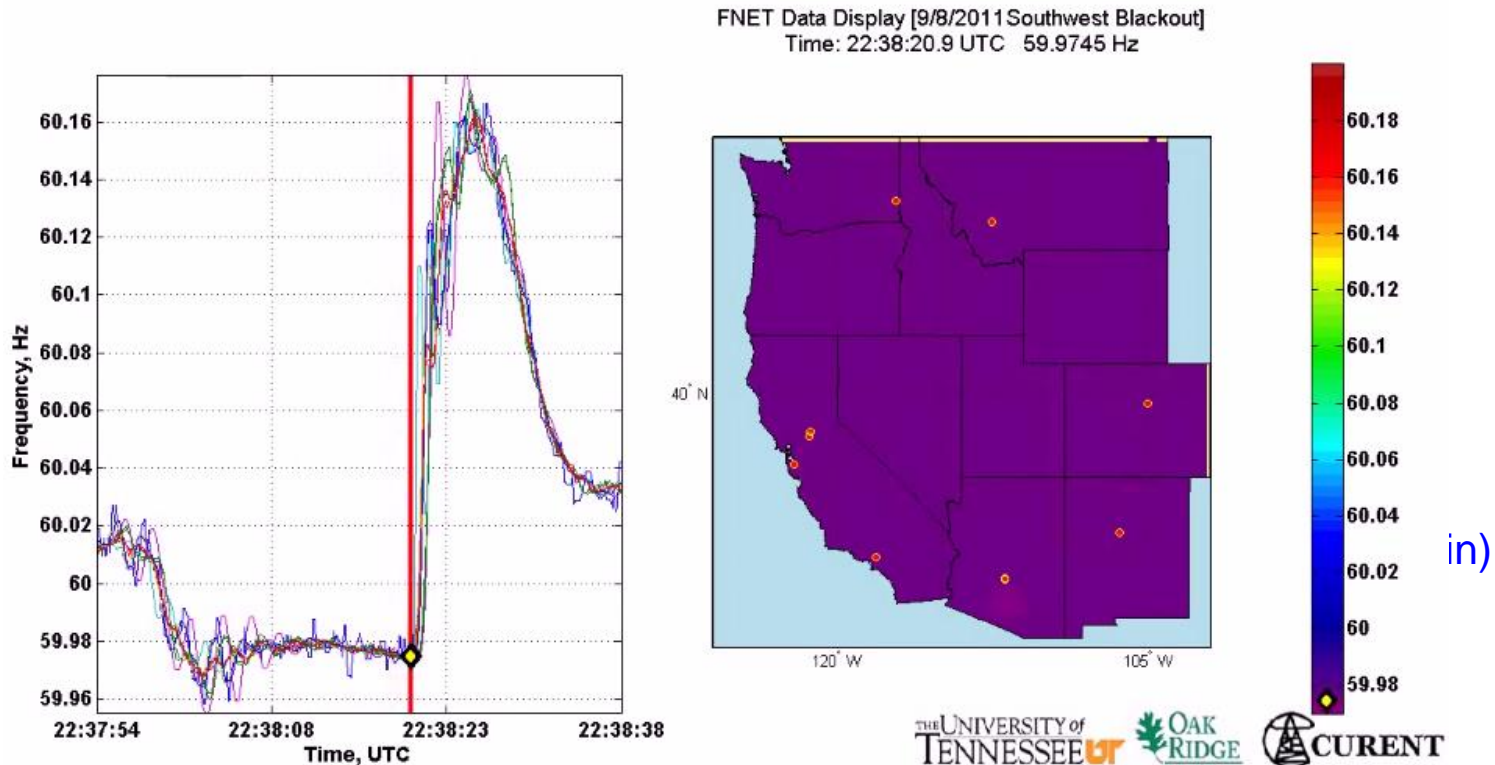
Applications





Motivation

- All buses synchronized to same nominal frequency (US: 60 Hz; Europe: 50 Hz)
- Supply-demand imbalance → frequency fluctuation

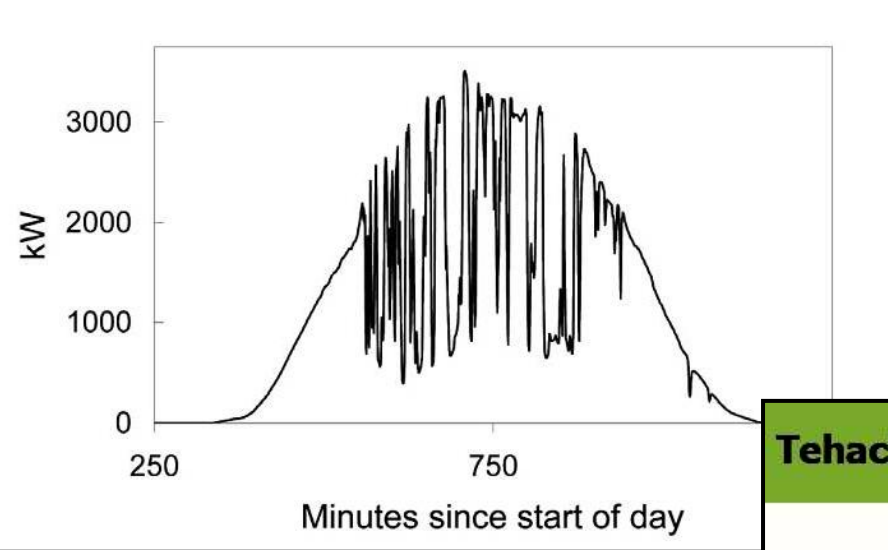


2011 Southwest blackout



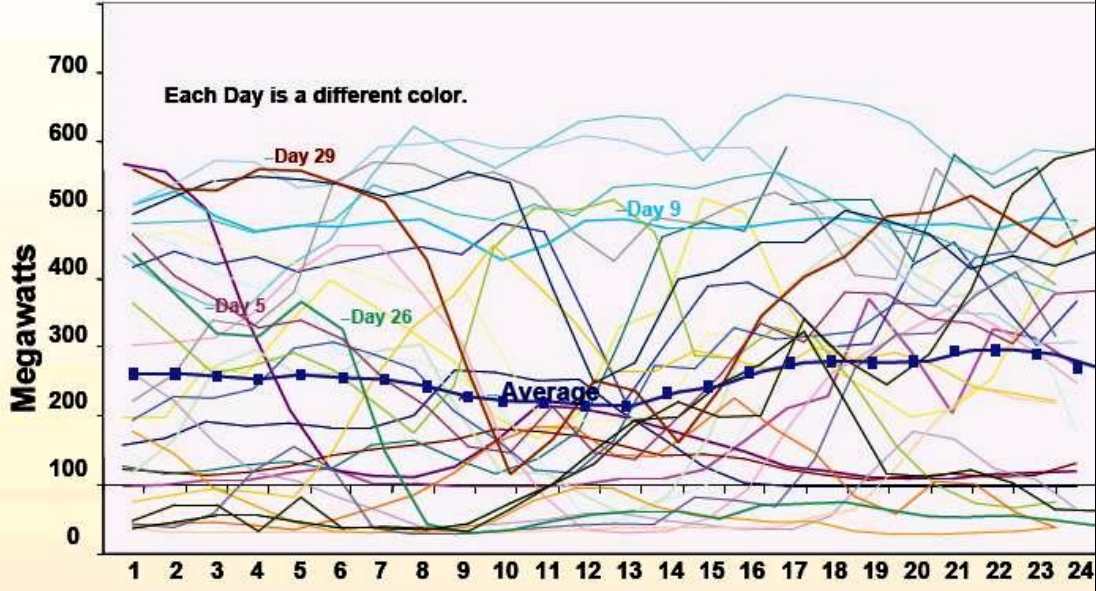
Motivation

Imagine when we have 33%+ renewable generation ...



Tehachapi Wind Generation in April – 2005

Could you predict the energy production for this wind park either day-ahead or 5 hours in advance?

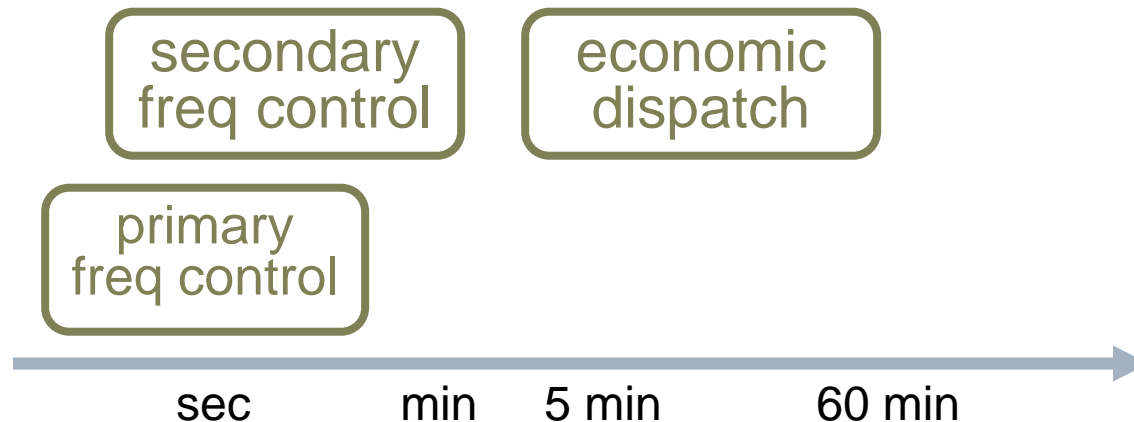




Frequency control

Traditionally done on generator-side

- primary: rebalance power, resynchronize freq
- secondary: restore nominal freq & inter-area flows
- tertiary (EC): maximize economic efficiency

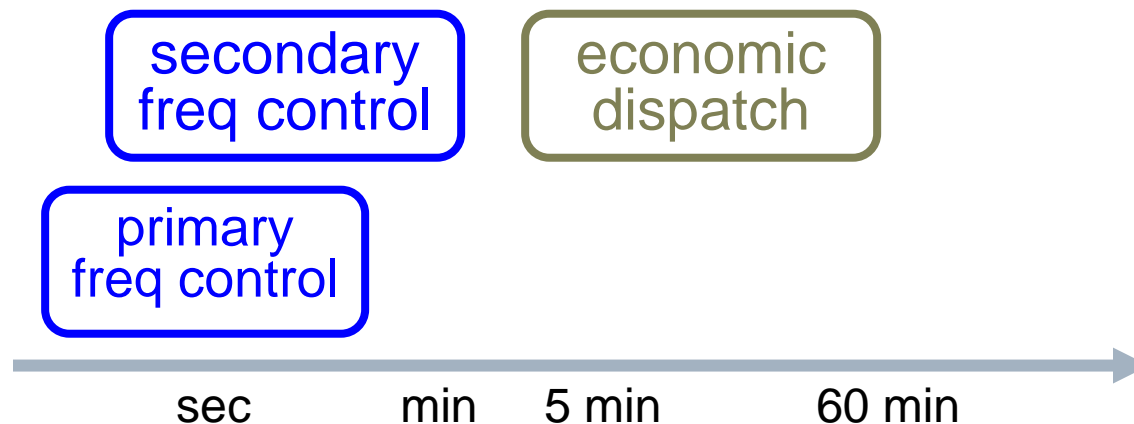




Why load-side participation

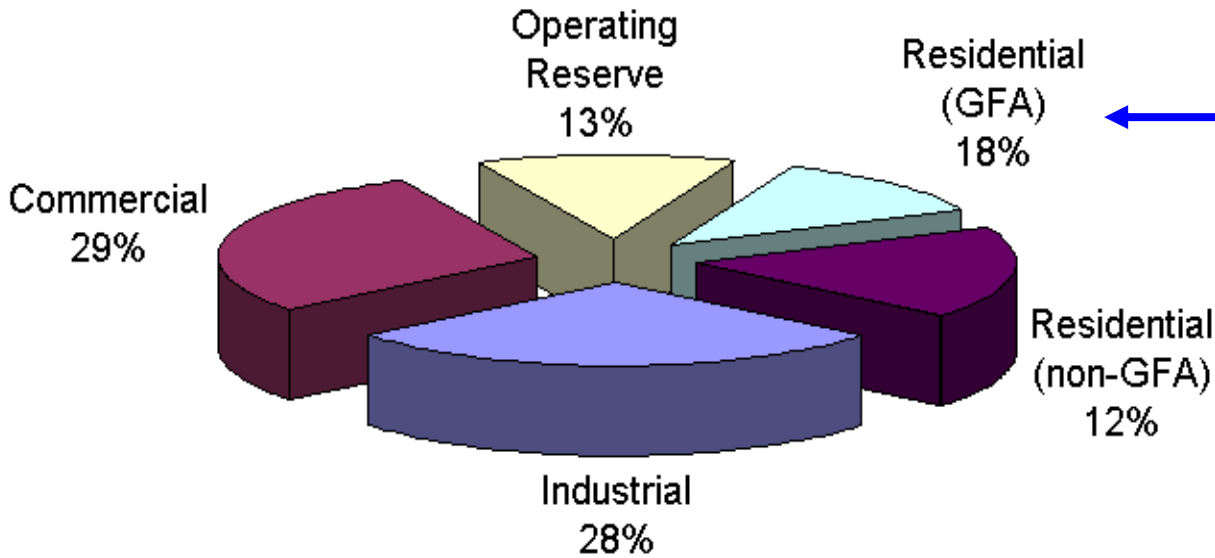
Ubiquitous continuous load-side control can supplement generator-side control

- faster (no/low inertia)
- no extra waste or emission
- more reliable (large #)
- better localize disturbances
- reducing generator-side control capacity



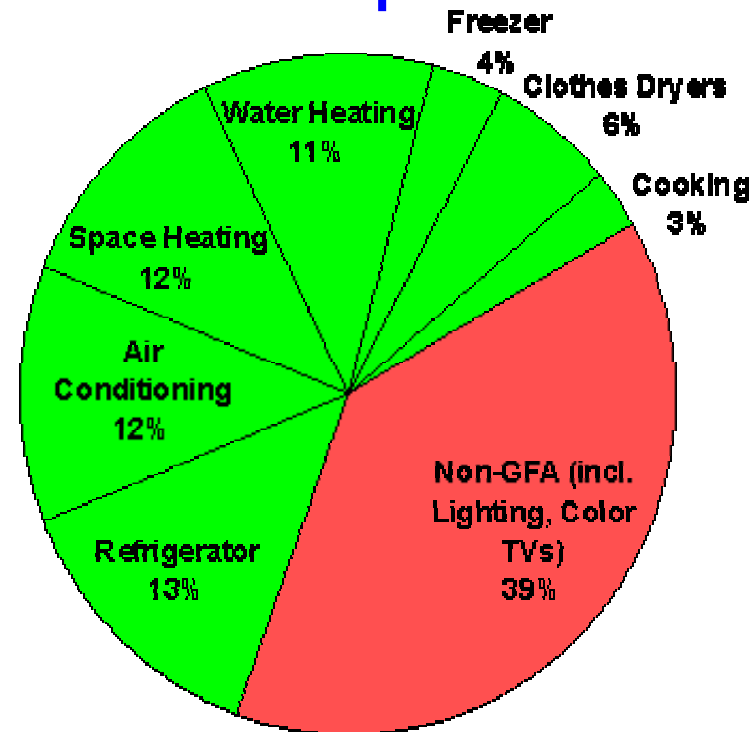


What is the potential



- Residential load accounts for ~1/3 of peak demand
- 61% residential appliances are Grid Friendly

US:
operating reserve: 13% of peak
total GFA capacity: 18%





How

How to design **load-side** frequency control ?

How does it interact with generator-side control ?



Literature: load-side control

Original idea

- Schweppe et al 1979, 1980

Small scale trials around the world

- D.Hammerstrom et al 2007, UK Market Transform Programme 2008

Numerical studies

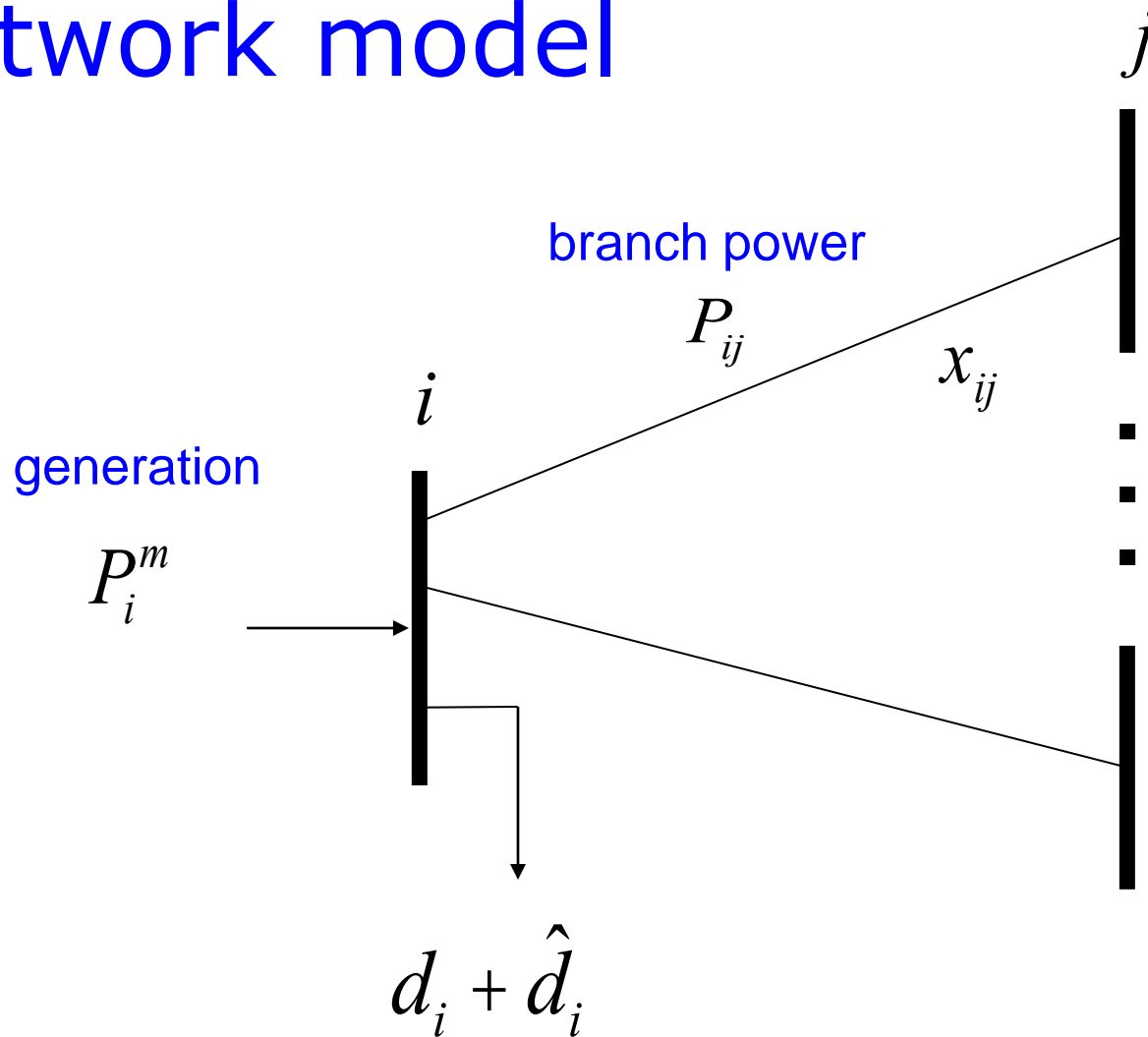
- Trudnowski et al 2006, Lu and Hammerstrom 2006, Short et al 2007, Donnelly et al 2010, Brooks et al 2010, Callaway and I. A. Hiskens, 2011, Molina-Garcia et al 2011

Analytical studies

- Zhao et al (2012/2014), Mallada et al (2014), Zhao and Low (2014)
- Simpson-Porco et al 2013, You and Chen 2014, Zhang and Papachristodoulou (2014), Zhao, et al (2014)



Network model



loads:
controllable + uncontrollable

i : region/control area/balancing authority



Dynamic model

$$\dot{\theta}_i = \omega_i$$

$$M_i \dot{\omega}_i = -D_i \omega_i + p_i - \sum_e C_{ie} P_e$$

$$P_{ij} = b_{ij} \sin(\theta_i - \theta_j) \quad \forall i \rightarrow j$$

generator bus: real power injection



Dynamic model

$$\dot{\theta}_i = \omega_i$$

$$M_i \dot{\omega}_i = -D_i \omega_i + p_i - \sum_e C_{ie} P_e$$

$$P_{ij} = b_{ij} \sin(\theta_i - \theta_j) \quad \forall i \rightarrow j$$

generator buses:

$$\dot{p}_i = -\frac{1}{\tau_{bi}} (p_i + a_i)$$

$$\dot{a}_i = -\frac{1}{\tau_{gi}} (a_i + p_i^c)$$

primary control $p_i^c(t) = p_i^c(\omega_i(t))$

e.g. freq droop $p_i^c(\omega_i) = -b_i \omega_i$



Dynamic model

$$\dot{\theta}_i = \omega_i$$

$$0 = -D_i \omega_i + d_i - \sum_e C_{ie} P_e$$

$$P_{ij} = b_{ij} \sin(\theta_i - \theta_j) \quad \forall i \rightarrow j$$

load bus: controllable load

how to design controller $d_i(t)$?

Proposed approach

- formalize control goals as OLC
- derive **distributed** control as primal-dual alg



Load-side controller design

$$\dot{\theta}_i = \omega_i$$

$$0 = -D_i \omega_i + d_i - \sum_e C_{ie} P_e$$

$$P_{ij} = b_{ij} \sin(\theta_i - \theta_j) \quad \forall i \rightarrow j$$

Control goals

Zhao, Topcu, Li,
Low
TAC 2014

Mallada, Zhao, Low
Allerton, 2014

- Rebalance power
- Stabilize frequency
- Restore nominal frequency
- Restore scheduled inter-area flows



Optimal load control (OLC)

$$\min_{d, \hat{d}, P, v} \sum_i \dot{a}_{\text{e}}^{\text{e}} c_i(d_i) + \frac{1}{2D_i} \hat{d}_i^2$$

$$\text{s. t.} \quad P^m - (d + \hat{d}) = CP \quad \text{demand = supply}$$

key idea: “virtual flows”

$$BC^T v$$

in steady state: virtual = real flows

$$BC^T v = P$$



Optimal load control (OLC)

$$\min_{d, \hat{d}, P, v} \quad \sum_i \dot{a}_i c_i(d_i) + \frac{1}{2D_i} \hat{d}_i^2$$

$$\text{s. t.} \quad P^m - (d + \hat{d}) = CP \quad \text{demand = supply}$$

$$P^m - d = CBC^T v \quad \text{restore nominal freq}$$

in steady state: virtual = real flows

$$BC^T v = P$$



Optimal load control (OLC)

$$\min_{d, \hat{d}, P, v} \quad \sum_i \dot{a}_{\text{e}}^{\text{e}} c_i(d_i) + \frac{1}{2D_i} \hat{d}_i^2 \ddot{\theta}$$

$$\text{s. t.} \quad P^m - (d + \hat{d}) = CP$$

demand = supply

$$P^m - d = CBC^T v$$

restore nominal freq

$$\hat{C}BC^T v = \hat{P}$$

restore inter-area flow

$$\underline{P} \preceq BC^T v \preceq \bar{P}$$

respect line limit

in steady state: virtual = real flows

$$BC^T v = P$$



Distributed load control

load control:
$$d_i(t) := \frac{\hat{c}_i}{\underline{c}_i} c_i^{-1} \left(W_i(t) + I_i(t) \right) \frac{\bar{d}_i}{\underline{d}_i}$$

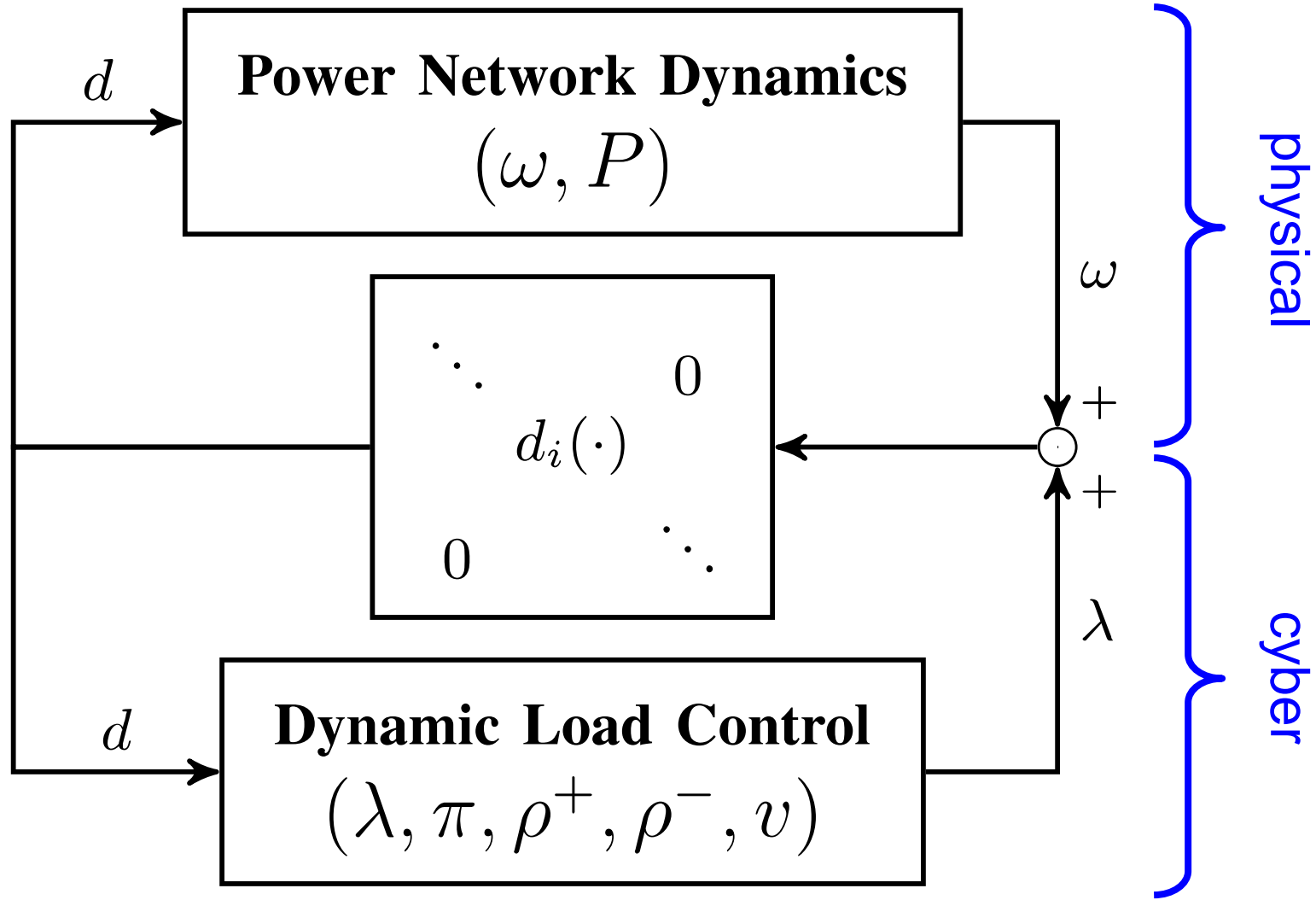
local frequency deviation
measured locally at load

virtual frequency
computed locally based
on neighborhood comm

network dynamics + active load control
= first-order primal-dual algorithm for OLC



Distributed control architecture





Load-side control works

Theorem

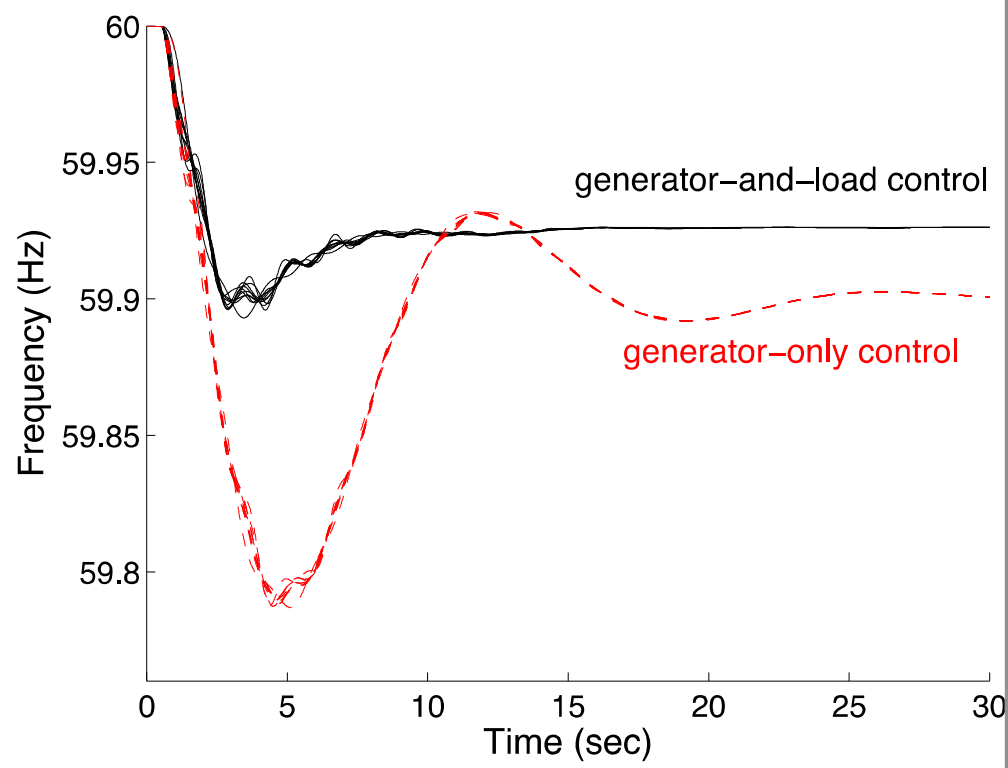
- Every closed-loop equilibrium solves OLC and its dual

Suppose $\left| p_i^c(w) - p_i^c(w^*) \right| \leq L_i \left| w - w^* \right|$

near w^* for some $L_i < D_i$

- Any closed-loop equilibrium is (locally) asymptotically stable provided

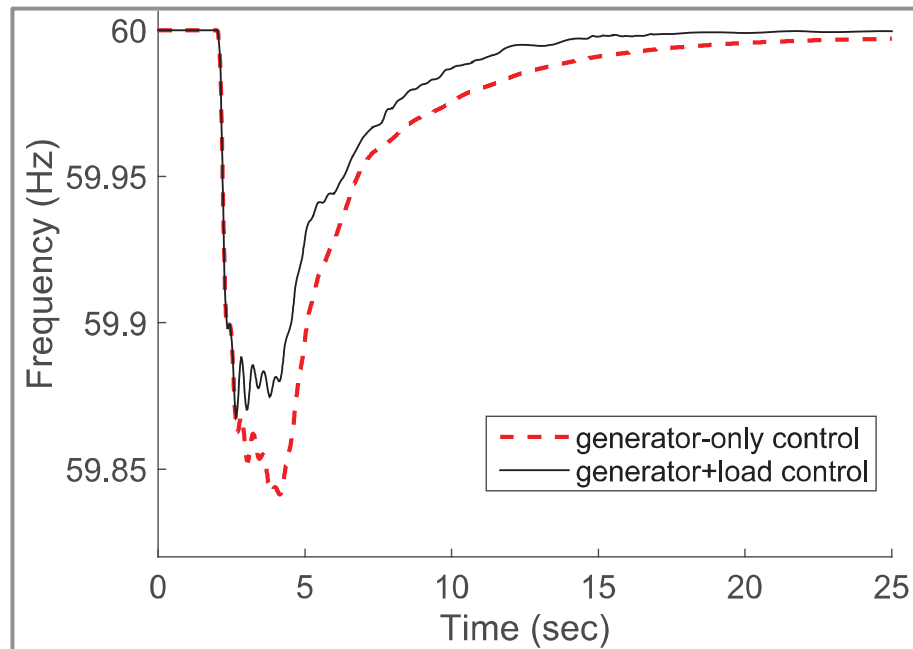
$$\left| q_i^* - q_j^* \right| < \frac{\rho}{2}$$



- Can replacing gen-side control with load-side control
- Load-side participation improves transient and steady state

PSS 39-bus, same control capacity
Primary frequency control

PSS 14-bus, same control capacity
Secondary frequency control





Recap

Forward-engineering design facilitates

- explicit control goals
- distributed algorithms
- stability analysis

Load-side frequency regulation

- essential as renewable replaces thermal gen
- improves generator-side control



Outline

Overview

Optimal power flow (OPF)

Frequency regulation

- problem formulation
- semidefinite relaxations
- exact relaxation

Applications





OPF research

2012

2013

2014

2015

2016

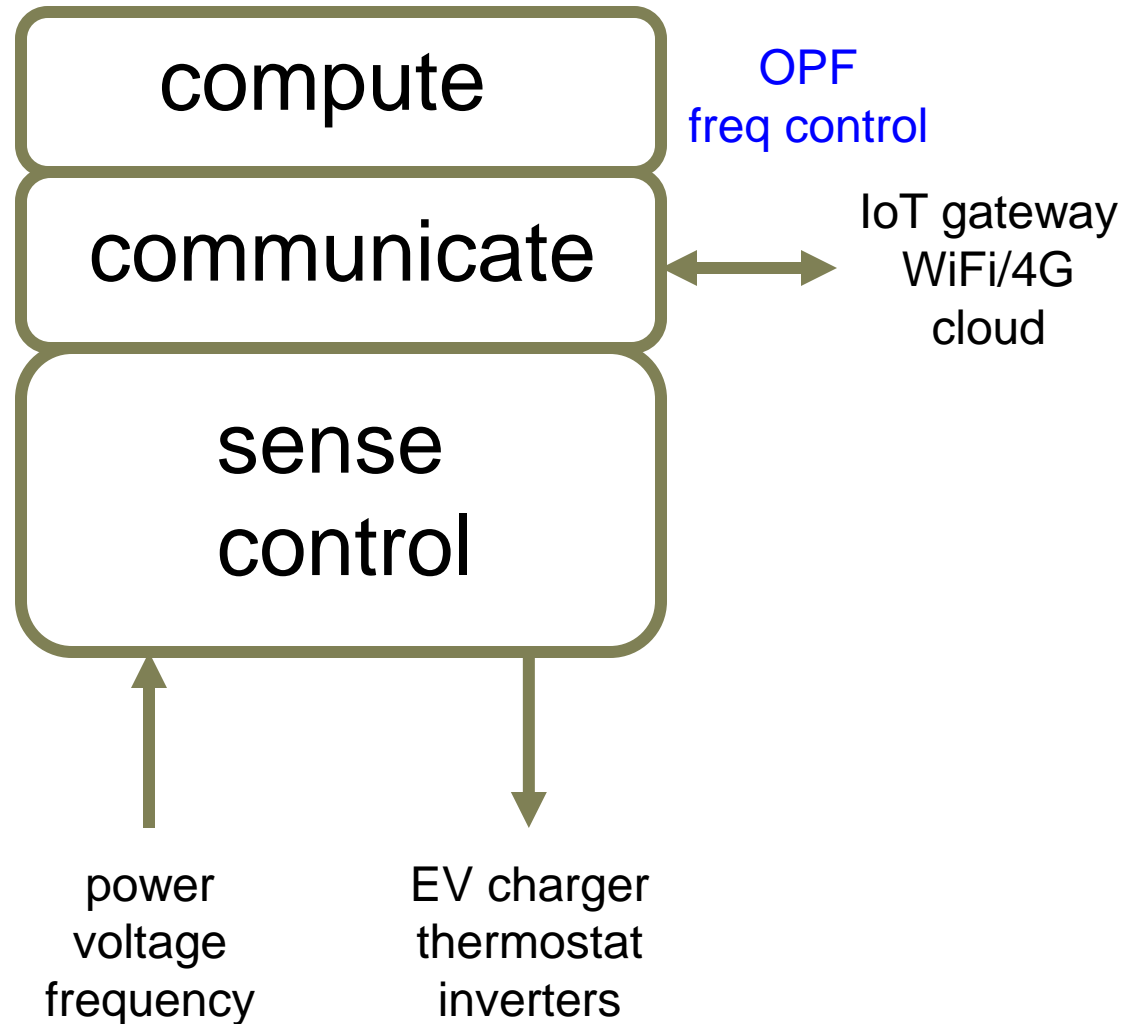
Theoretical foundation
semidefinite relaxations of OPF

Algorithm design
unbalanced OPF, distributed OPF

Implementation & T2M
IoT gateway, testbed, field test

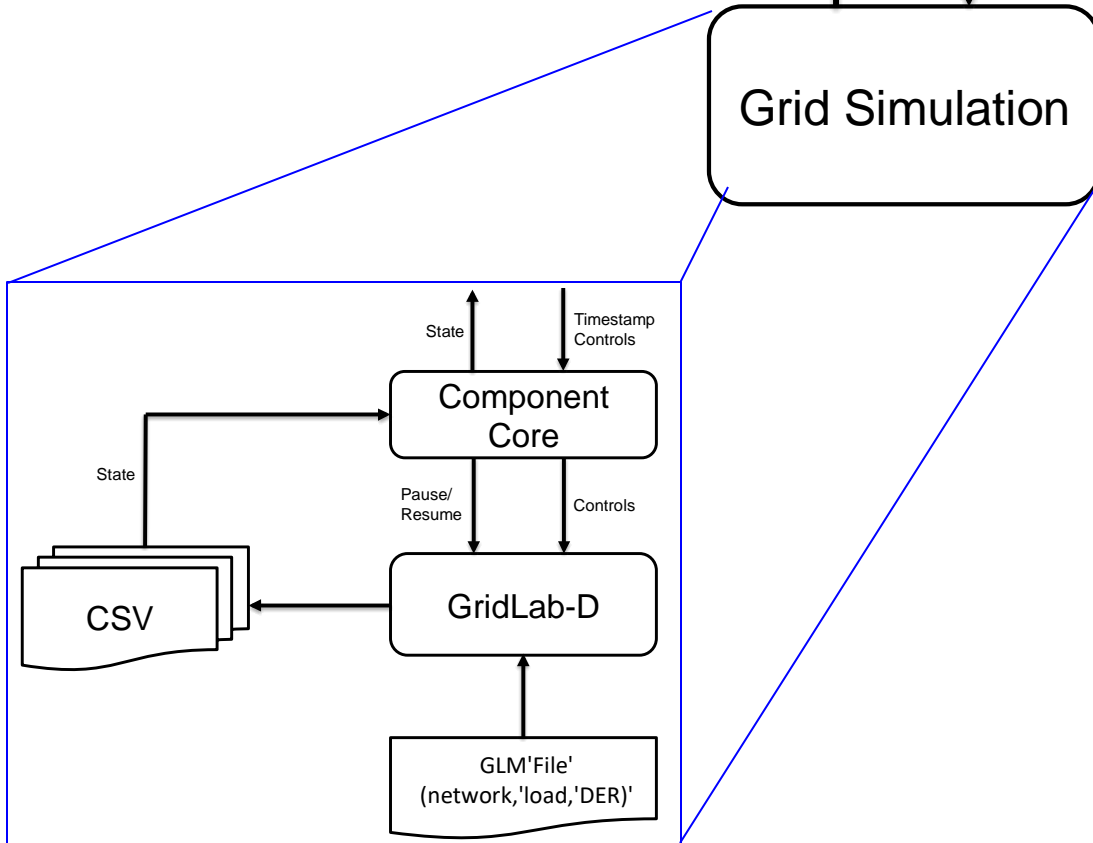
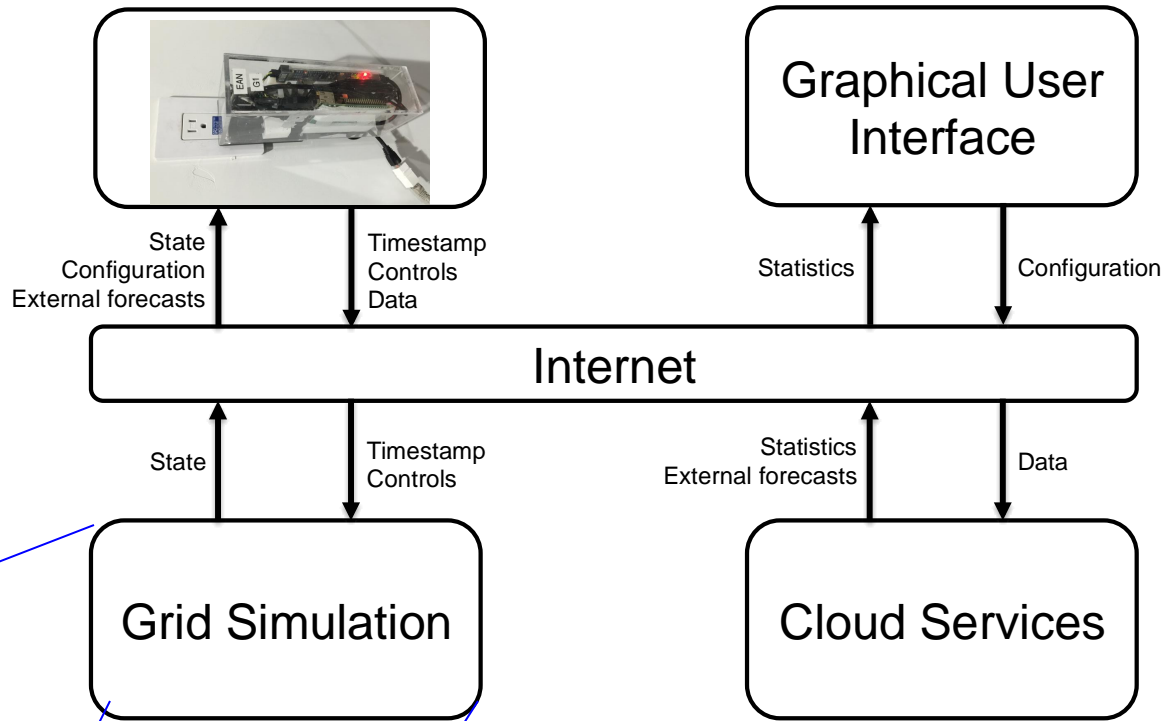


IoT gateway prototype



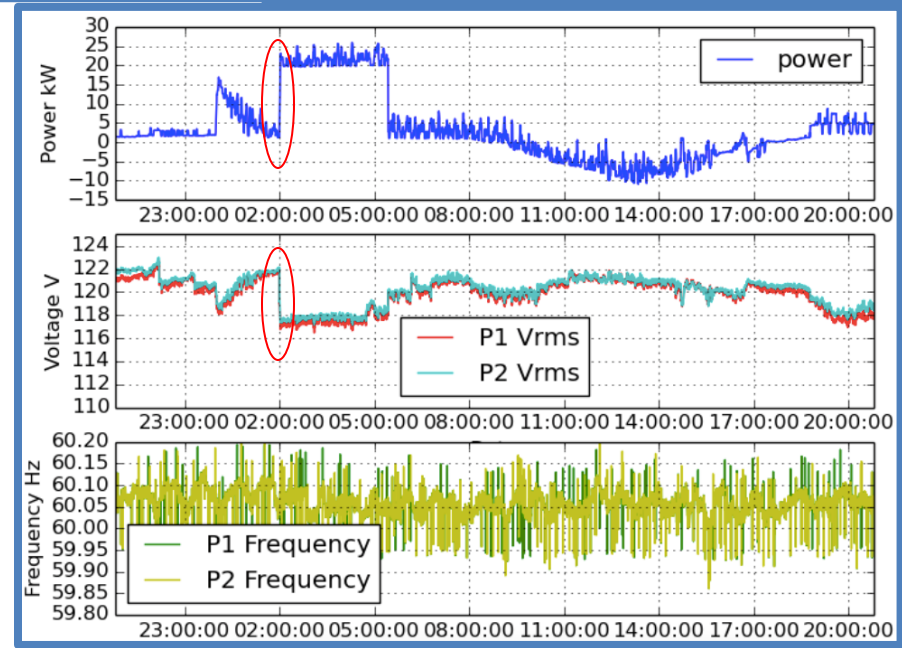
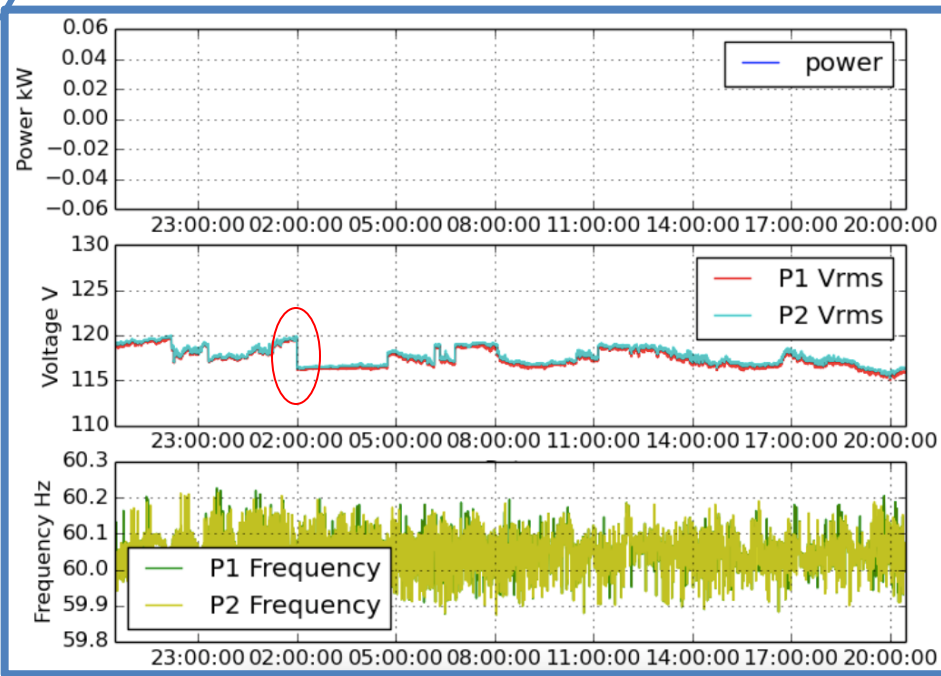
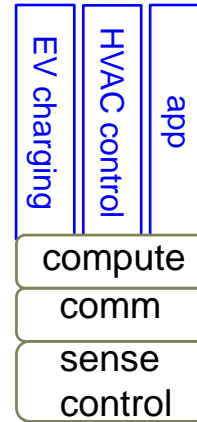
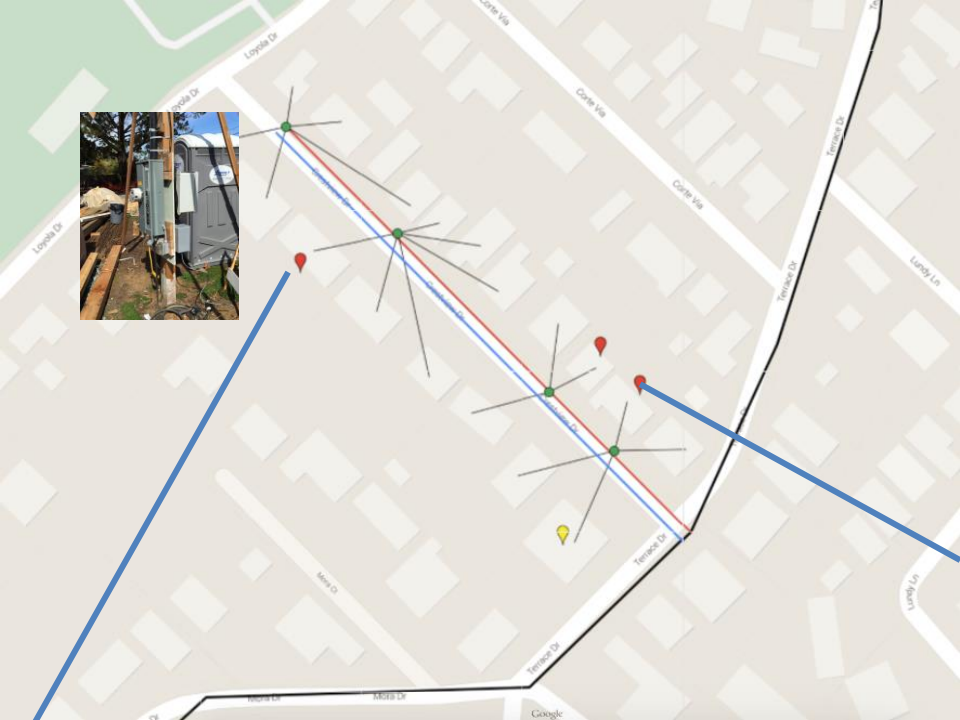


Testbed



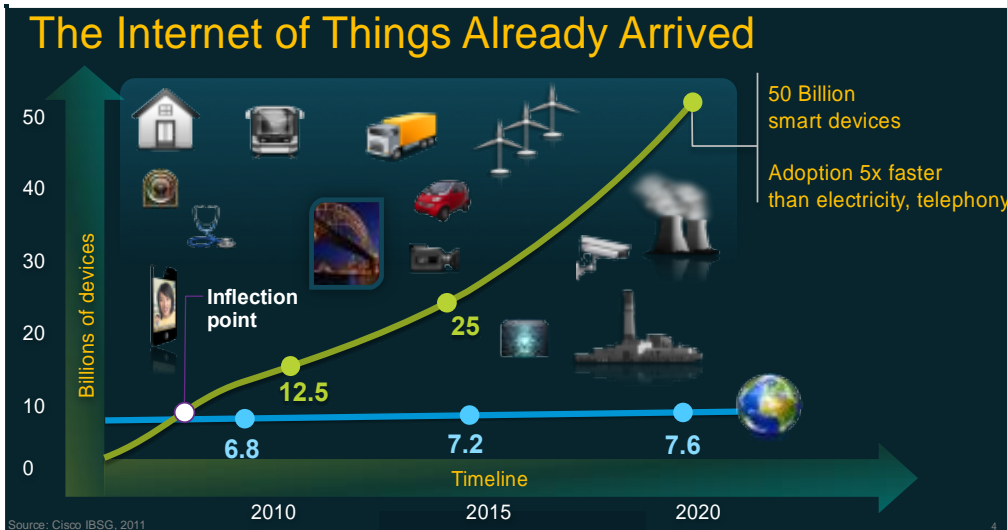
Field test

George Lee

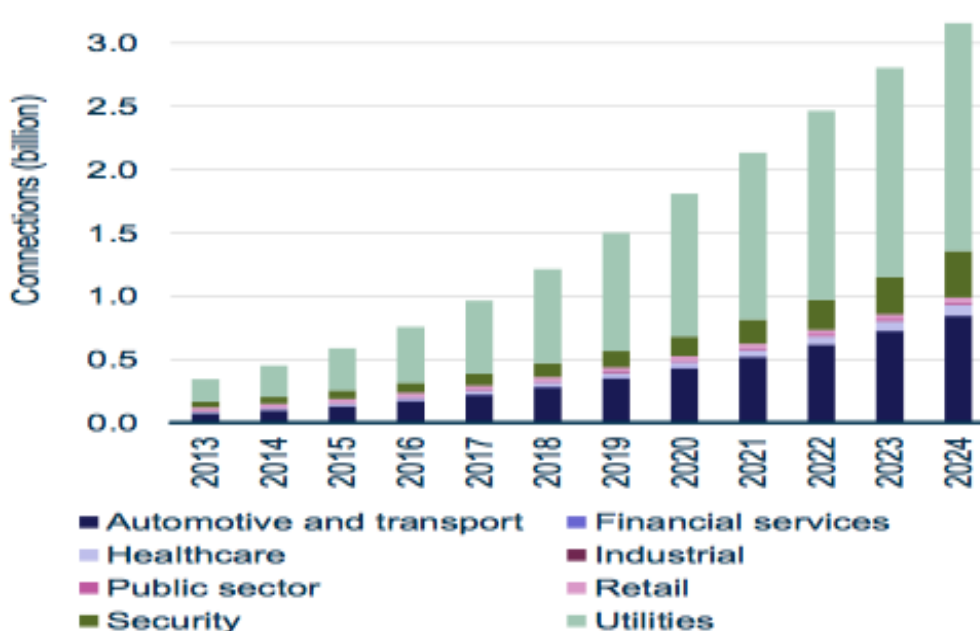




Tech-to-market



IoT has been growing at unprecedented rate

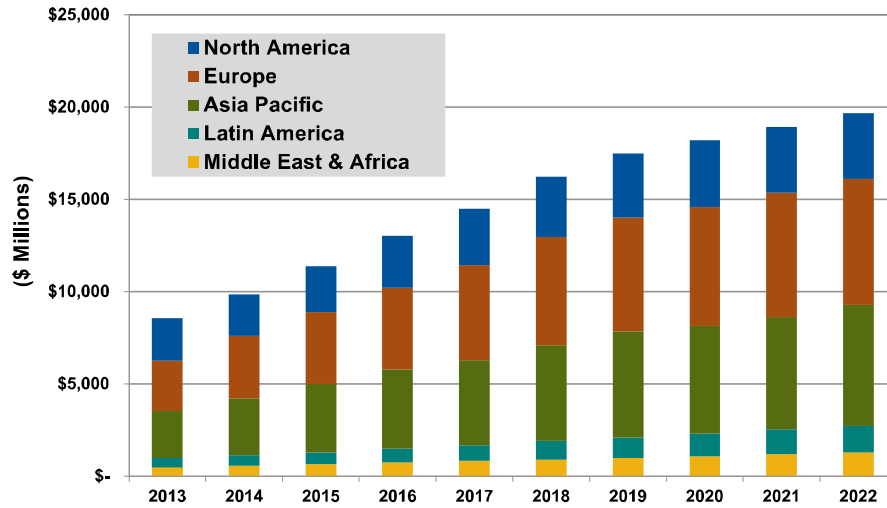


Energy is the largest application for IoT



Tech-to-market

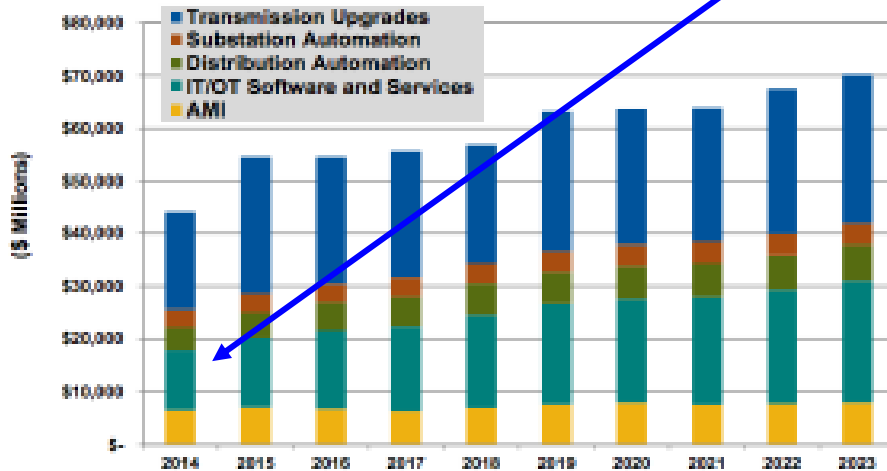
6.2.2 Smart Grid IT Software and Services Spending by Region, World Markets: 2013-2022



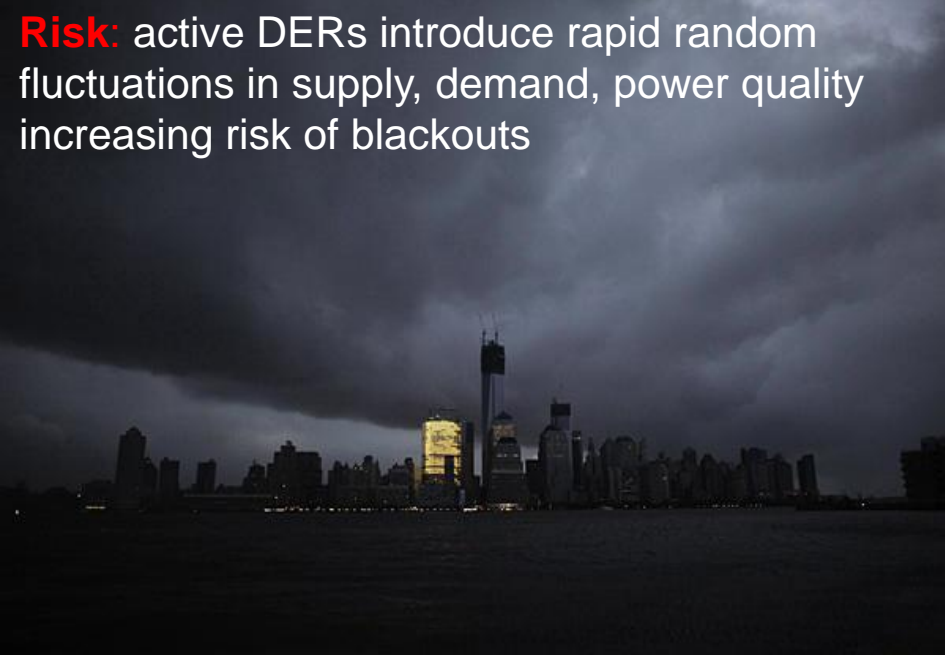
(Source: Navigant Research)

SG IT software is already a multi-B market

6.2 Smart Grid Technology Revenue by Application, World Markets: 2014-2023



(Source: Navigant Research)

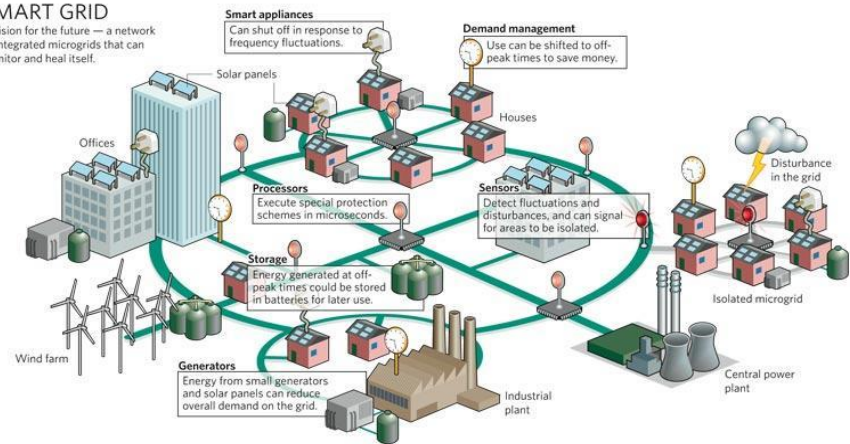


Risk: active DERs introduce rapid random fluctuations in supply, demand, power quality increasing risk of blackouts

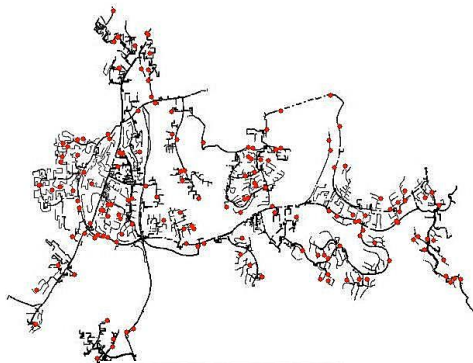
Opportunity: active DERs enables realtime dynamic network-wide feedback control, improving robustness, security, efficiency

SMART GRID

A vision for the future — a network of integrated microgrids that can monitor and heal itself.



Caltech research: distributed control of networked DERs



- Foundational theory, practical algorithms, concrete applications
- Integrate engineering and economics
- Active collaboration with industry

